宇宙線による星間媒質の不安定的加熱機構の可能性について

霜田治朗

高エネルギー現象で探る宇宙の多様性(2024/11/12)

Collaborators (予定): Y. Ohira, K. Asano, S. Inutsuka

Roles of Galactic Cosmic Rays



"Puzzling" Star Formation History (the metal amount)



(a) disk $SFR \sim 3 Mo/yr$

Gas mass ~ 10^9 Mo (Metallicity Zo ~ $0.01 \rightarrow$ Metal mass ~ 10^7 Mo) Salpeter IMF \rightarrow Massive Star FR ~ 0.1 Mo/yr

Total Metal Mass Ejected by SNe

 $\rightarrow \sim$ (SFR) x (Massive Star fraction) x (CO core mass fraction) x (14 Gyr) ~ (3 Mo/yr) x (0.1) x (3 Mo/8 Mo) x (14 Gyr) ~1.6 x 10⁹ Mo

~99 % of metals should be removed from the disk! \rightarrow Persistent Outflow is required! (SJ & Inutsuka 22, SJ, Inutsuka, & Nagashima 24, SJ & Asano 24)





Outflow: T ~ 0.1 keV (~virial temp. of the MW) →eROSITA bubble is consistent with this expectation. Should be launched at the disk (removing the metals) → Formation mechanism is unclear...



宇宙線の逃走問題(拡散係数問題)

Diffusive Shock Acceleration (DSA) →衝撃波を往復して粒子が加速していく

→Vshが小さくなると、衝撃波が拡散する 宇宙線に追いつけない.

→宇宙線が上流に**逃走して加速終了**.

downstream \rightarrow subscript "2"

「いつ,どれだけ逃走しているのか?」は 分かっていない.

Supernova Remnants: Temporal Evolution

G1.9+0.3: Youngest SNR in our Galaxy (age~140 yr, Bamba & Williams 22) Free Expansion Phase



~ Late Sedov phase (w/ clear Reverse shock)

SNR DEM L71 @LMC (X-ray), age~a few kyr

~ Snowplow phase (T<0.1 keV or Vsh < 300 km/s)

SNR Cygnus Loop (UV), age~10 kyr



G70.0-21.5 Blue OIII, Red H α age ~ 10-100 kyr?

Cooling function by SJ et al. 22 (high-Temp. side) + Koyama & Inutsuka O2 (low-Temp. side)





・SNRから離れたところでISMが加熱されるなどが起こりうる。

・CR加熱率(升)は色々提案されている(e.g., Acterberg+81, Zweibel 20, Yokoyama & Ohira 23)が、 実際のところよく分かっていない。

$$\mathcal{H} < \mathcal{H}_0,$$

 $\mathcal{H}_0 = e_{\rm cr}/\tau_{\rm res} = 1.8 \times 10^{-26} \,{\rm erg} \,{\rm cm}^{-3} \,{\rm s}^{-1} (e_{\rm cr}/1 \,{\rm eV/cc}) (\tau_{\rm res}/1 \,{\rm Myr})^{-1}.$

The CR-hydrodynamics

$$\frac{\partial \rho}{\partial t} + \boldsymbol{\nabla} \left(\rho \boldsymbol{v} \right) = 0$$
$$\rho \frac{d \boldsymbol{v}}{d t} = -\boldsymbol{\nabla} \left(P_{\rm g} + P_{\rm cr} \right)$$

 $P_{\rm g}$ is the pressure of thermal gas $P_{\rm cr}$ is the CR pressure

The energy equation is ...

$$dQ = d(E_{g} + E_{cr}) + (P_{g} + P_{cr})dV$$
$$dQ_{rad} + dQ_{conv} + dQ_{vis} + dQ_{cr} + \dots$$

The 1st law of thermodynamics should include the CRs

Radiation, (thermal) convection, viscosity, CRs energy interactions, …

The CR-hydrodynamics: the energy equation

$$P_{\rm g} = (\gamma_{\rm g} - 1)e_{\rm g} = 2e_{\rm g}/3$$

 $P_{\rm cr} = (\gamma_{\rm cr} - 1)e_{\rm cr} = e_{\rm cr}/3$

The CR-hydrodynamics: the energy equation

$$\begin{aligned} \frac{dP_{\rm g}}{dt} - C_{\rm g}^2 \frac{d\rho}{dt} &= G(\rho, T, P_{\rm cr}) \\ \frac{dP_{\rm cr}}{dt} - C_{\rm cr}^2 \frac{d\rho}{dt} &= R(\rho, T, P_{\rm cr}) \end{aligned}$$
$$\begin{aligned} C_{\rm cr} &= \sqrt{\frac{\gamma_{\rm cr} P_{\rm cr}}{\rho}} \\ R(\rho, T, P_{\rm cr}) &= \nabla \cdot (\mathcal{D} \nabla P_{\rm cr}) - \gamma_* \mathcal{H}, \\ \gamma_* &= \frac{\gamma_{\rm cr} - 1}{\gamma_{\rm g} - 1} = \frac{1}{2}, \end{aligned}$$

 $P_{\rm g} = (\gamma_{\rm g} - 1)e_{\rm g} = 2e_{\rm g}/3$

 $P_{\rm cr} = (\gamma_{\rm cr} - 1)e_{\rm cr} = e_{\rm cr}/3$

$$C_{g} = \sqrt{\frac{\gamma_{g}P_{g}}{\rho}},$$

$$G(\rho, T, P_{cr}) = \mathcal{L}^{*}(\rho, T) + \nabla \cdot (\mathcal{K}^{*}\nabla T) + \mathcal{H},$$

$$\mathcal{L}^{*}(\rho, T) = (\gamma_{g} - 1)\mathcal{L}_{rad,g}(\rho, T),$$

$$\mathcal{H}(\rho, T, P_{cr}) = (\gamma_{g} - 1)\mathcal{L}_{em,cr}(\rho, T, P_{cr}),$$
Energy Exchange effect
$$\frac{d(P_{g} + P_{cr})}{dt} - (C_{g}^{2} + C_{cr}^{2})\frac{d\rho}{dt} \sim (1 - \gamma_{*})\mathcal{H}$$

The CR-hydrodynamics: the energy equation

$$P_{\rm g} = (\gamma_{\rm g} - 1)e_{\rm g} = 2e_{\rm g}/3$$

 $P_{\rm cr} = (\gamma_{\rm cr} - 1)e_{\rm cr} = e_{\rm cr}/3$

The CR heating produces additional total pressure!

$$\mathcal{P} = P_{g} + P_{cr} = \mathcal{P}(e_{g} + |e_{1}|, e_{cr} - |e_{1}|)$$
$$= \mathcal{P}(e_{g}, e_{cr}) + \frac{|e_{1}|}{3}$$

What happens?? \rightarrow Linear analysis

The CR-hydrodynamics: Linear Analysis in uniform medium



CRs supplied by the source (SNR)

$$\mathcal{Q}_{\text{ex}} = \mathcal{H} = \frac{\mathcal{H}_0}{10}$$
$$\mathcal{H}_0 = \frac{e_{\text{cr}}}{\tau_{\text{res}}} = 1.8 \times 10^{-26} \text{ erg cm}^{-3} \text{ s}^{-1} \left(\frac{e_{\text{cr}}}{1 \text{ eV/cc}}\right) \left(\frac{\tau_{\text{res}}}{1 \text{ Myr}}\right)^{-1}$$

Equilibrium condition $n\Gamma - n^2 \Lambda(T) + \mathcal{H} = 0$



The CR-hydrodynamics: Linear Analysis in uniform medium



Equilibrium condition $n\Gamma - n^2\Lambda(T) + \mathcal{H} = 0$



$$\frac{\partial \rho}{\partial t} + \boldsymbol{\nabla} \left(\rho \boldsymbol{v} \right) = 0$$
$$\rho \frac{d \boldsymbol{v}}{d t} = -\boldsymbol{\nabla} \left(P_{\rm g} + P_{\rm cr} \right)$$

$$\frac{dP_{\rm g}}{dt} - C_{\rm g}^2 \frac{d\rho}{dt} = G(\rho, T, P_{\rm cr})$$
$$\frac{dP_{\rm cr}}{dt} - C_{\rm cr}^2 \frac{d\rho}{dt} = R(\rho, T, P_{\rm cr})$$

$$\begin{split} G_r &= \partial_{\rho}G - \frac{\mathcal{T}}{\rho}\partial_{\mathcal{T}}G \\ &= \Gamma^* - \rho\Lambda^* (2-\chi) + \frac{\mathcal{H}}{\rho} (\eta_r - \eta_{\mathcal{T}}) - \frac{\mathcal{K}^*\mathcal{T}}{\rho} \boldsymbol{\nabla}^2, \\ G_p &= \frac{\partial_{\mathcal{T}}G}{\rho} = -\frac{\rho\Lambda^*}{\mathcal{T}}\chi + \frac{\mathcal{H}}{\rho\mathcal{T}}\eta_{\mathcal{T}} + \frac{\mathcal{K}^*}{\rho} \boldsymbol{\nabla}^2, \\ G_q &= \frac{\mathcal{H}}{P_{\rm cr}}\eta_q, \\ R_r &= -\frac{\gamma_*\mathcal{H}}{\rho} (\eta_r - \eta_{\mathcal{T}}), \\ R_p &= -\frac{\gamma_*\mathcal{H}}{\rho\mathcal{T}}\eta_{\mathcal{T}}, \\ R_q &= -\frac{\gamma_*\mathcal{H}}{P_{\rm cr}}\eta_q + \mathcal{D}\boldsymbol{\nabla}^2, \\ \chi &= \frac{\Lambda}{\mathcal{T}}\frac{\partial\Lambda}{\partial\mathcal{T}} = \frac{\partial\ln\Lambda}{\partial\ln\mathcal{T}}, \\ \eta_r &= \frac{\partial\ln\mathcal{H}}{\partial\ln\rho}, \eta_{\mathcal{T}} = \frac{\partial\ln\mathcal{H}}{\partial\ln\mathcal{T}}, \eta_q = \frac{\partial\ln\mathcal{H}}{\partial\ln P_{\rm cr}}, \end{split}$$

$$\begin{bmatrix} \partial_t^2 \left(\partial_t^2 - C_*^2 \boldsymbol{\nabla}^2 \right) & - & \partial_t \left(\nu \partial_t^2 + \dot{\epsilon} \boldsymbol{\nabla}^2 \right) \\ - & \left(\dot{\nu} \partial_t^2 - \ddot{\epsilon} \boldsymbol{\nabla}^2 \right) \end{bmatrix} P_{\mathrm{g},1} = 0,$$

$$\nu = G_p + R_q$$

$$\dot{\epsilon} = G_r + R_r + (R_p - R_q) C_g^2 + (G_q - G_p) C_{cr}^2$$

$$\dot{\nu} = G_q R_p - G_p R_q$$

$$\ddot{\epsilon} = (R_q - R_p) G_r + (G_p - G_q) R_p$$

$$C_* = \sqrt{C_{\rm g}^2 + C_{\rm cr}^2}$$

$$\frac{dP_{\rm g}}{dt} - C_{\rm g}^2 \frac{d\rho}{dt} = G(\rho, T, P_{\rm cr})$$
$$\frac{dP_{\rm cr}}{dt} - C_{\rm cr}^2 \frac{d\rho}{dt} = R(\rho, T, P_{\rm cr})$$

Know as Thermal Instability (Field 65)

$$\begin{bmatrix} \partial_t^2 \left(\partial_t^2 - C_*^2 \nabla^2 \right) & - & \partial_t \left(\nu \partial_t^2 + \dot{\epsilon} \nabla^2 \right) \\ & - & \left(\dot{\nu} \partial_t^2 - \ddot{\epsilon} \nabla^2 \right) \end{bmatrix} P_{g,1} = 0,$$

$$\nu = G_p + R_q$$

$$\dot{\epsilon} = G_r + R_r + (R_p - R_q) C_g^2 + (G_q - G_p) C_{cr}^2$$

$$\dot{\nu} = G_q R_p - G_p R_q$$

$$\ddot{\epsilon} = (R_q - R_p) G_r + (G_p - G_q) R_q$$

Sound Waves

 $C_* = \sqrt{C_{\rm g}^2 + C_{\rm cr}^2}$

$$\frac{dP_{\rm g}}{dt} - C_{\rm g}^{2} \frac{d\rho}{dt} = G(\rho, T, P_{\rm cr})$$
$$\frac{dP_{\rm cr}}{dt} - C_{\rm cr}^{2} \frac{d\rho}{dt} = R(\rho, T, P_{\rm cr})$$



$$\nu = G_p + R_q$$

$$\dot{\epsilon} = G_r + R_r + (R_p - R_q) C_g^2 + (G_q - G_p) C_{cr}^2$$

$$\dot{\nu} = G_q R_p - G_p R_q$$

$$\ddot{\epsilon} = (R_q - R_p) G_r + (G_p - G_q) R_q$$

$$\frac{dP_{\rm g}}{dt} - C_{\rm g}^2 \frac{d\rho}{dt} = G(\rho, T, P_{\rm cr})$$
$$\frac{dP_{\rm cr}}{dt} - C_{\rm cr}^2 \frac{d\rho}{dt} = R(\rho, T, P_{\rm cr})$$



Sound Waves

Oscillating Force

$$\partial_t^2 \left(\partial_t^2 - C_*^2 \nabla^2 \right) P_{g,1} = \dot{\nu} \left(\partial_t^2 - \frac{\ddot{\epsilon}}{\dot{\nu}} \nabla^2 \right) P_{g,1}$$

$$\ddot{x} = -\omega^2 x + f_0 \cos(\omega_0 t)$$
$$x(t) = A \cos(\omega t) + f_0 \frac{\cos(\omega_0 t) - \cos(\omega t)}{\omega^2 - \omega_0^2}$$

Making Oscillation

Like Forced Oscillation \rightarrow Eigenvectors may show kind of resonance

$$\begin{aligned} \xi_q &\equiv \frac{P_{\mathrm{cr},1}/P_{\mathrm{cr}}}{P_{\mathrm{g},1}/P_{\mathrm{g}}} \\ &= \frac{(\mathrm{i}\omega + G_p)(\mathrm{i}\omega C_{\mathrm{cr}}^2 - R_r) - R_p(\mathrm{i}\omega C_{\mathrm{g}}^2 - G_r)}{(\mathrm{i}\omega + R_q)(\mathrm{i}\omega C_{\mathrm{g}}^2 - G_r) - G_q(\mathrm{i}\omega C_{\mathrm{cr}}^2 - R_r)} \frac{P_{\mathrm{g}}}{P_{\mathrm{cr}}}, \\ \xi_\rho &\equiv \frac{\rho_1/\rho}{P_{\mathrm{g},1}/P_{\mathrm{g}}} = \frac{\rho_1 \mathcal{T}}{P_{\mathrm{g},1}} \left(1 + \frac{P_{\mathrm{cr},1}}{P_{\mathrm{g},1}}\right), \\ \xi_\mathcal{T} &\equiv \frac{\mathcal{T}_1/\mathcal{T}}{P_{\mathrm{g},1}/P_{\mathrm{g}}} = 1 - \frac{\rho_1 \mathcal{T}}{P_{\mathrm{g},1}}, \\ \xi_v &\equiv \frac{\rho C_{\mathrm{g}} v_1}{P_{\mathrm{g},1}} = \frac{k_c C_{\mathrm{g}}}{\omega} \left(1 + \frac{P_{\mathrm{cr},1}}{P_{\mathrm{g},1}}\right). \end{aligned}$$









Outflow Launching?





NOT SIMPLE @ T ~ 0.1 keV scale...

Fesen et al. 2024 report [OIII] λ 5007 (in old SNRs)



The CR heating effect explains such emission?

Hadronic γ -ray observed?

Future work

1st ionization potentials: O^{+1} →35 eV O^{+2} →55 eV O^{+3} →77 eV

Summary

The Galactic Wind

- Invoked to explain metals in/around galaxies.
- Possibly explain eROSITA bubble & Fermi bubble simultaneously.
- We must find the formation mechanism of the "seed gas" in the disk.

The effects of CR heating

- The heating can be seen like forced oscillation (damped within ~0.1 Myr).
- Possibly work around CR sources like SNRs/PWNe.
- Details are still not derived.

$$\mathcal{P} = P_{g} + P_{cr} = \mathcal{P}(e_{g} + |e_{1}|, e_{cr} - |e_{1}|)$$
$$= \mathcal{P}(e_{g}, e_{cr}) + \frac{|e_{1}|}{3}$$



Reason is Simple