

# Kneeの起源についての一考察 - 銀河系外宇宙線からの寄与 -

Origin of the knee in the cosmic ray spectrum  
- Contribution from the extragalactic cosmic rays -

24 Jan. 2003 ICRR Seminar

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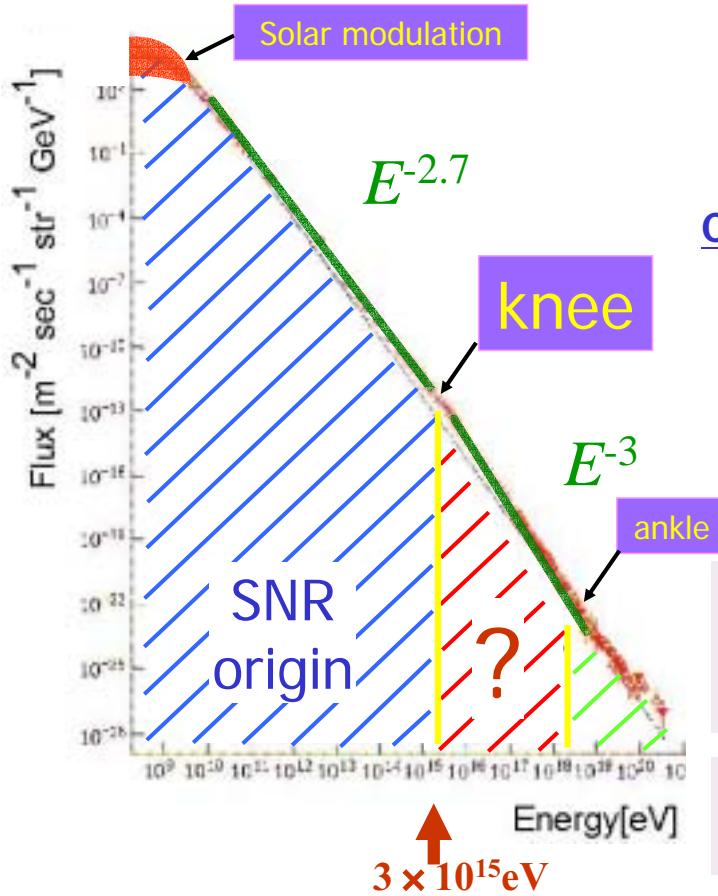
### 3. A model of the all-particle spectrum near the knee region

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- Energetics of hypothetical extragalactic CRs
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# 1. Introduction



## Cosmic rays (CRs)

Relativistic particles reaching the Earth from space  
(p 90%, He 9%,...)

## CR spectrum

Power law spectrum  
 $\sim E^{-2.7}$  ( $< 3 \times 10^{15}$  eV)  
 $\sim E^{-3.0}$  ( $3 \times 10^{15} - 10^{18}$  eV)  
 Spectral break around  $10^{15}$  eV  
 (referred to as the 'knee')

CRs below the 'knee' have been believed to be originated in **Supernovae** in our Galaxy !

CRs above the 'knee' is still unsettled !

## General arguments of the Supernovae Origin of Galactic CRs

### (1) Energetics (Hayakawa 1952, etc.)

✧ Generating power of CRs

$$P_{\text{CR}} \approx 10^{40} \left( \frac{\text{CR}}{10^{-12} \text{ erg cm}^{-3}} \right) \left( \frac{V}{10^{67} \text{ cm}^3} \right) \left( \frac{\text{CR}}{10^7 \text{ yr}} \right)^{-1} \text{ erg s}^{-1}$$

✧ Power supply by SNe

$$P_{\text{SNR}} \approx 10^{42} \left( \frac{E_{\text{CR}}}{10^{-51} \text{ erg}} \right) \left( \frac{\text{SN-rate}}{1/30 \text{ yr}^{-1}} \right) \text{ erg s}^{-1} \quad P_{\text{CR}} \sim 0.01 P_{\text{SNR}}$$

### (2) CR energy spectrum (Bell 1978, etc.)

✧ Observed energy spectrum  $E^{-2.7}$

✧ Expected energy spectrum from the diffusive shock acceleration in SNR

$$E^{-\frac{r_c + 2}{r_c - 1}}$$

**SNRs have the necessary power and the Fermi shock acceleration mechanism provides the observed spectrum.**

### (3) Elemental and Isotopic Composition

(Yanagita, Hayakawa & Nomoto 1990)

## Direct evidence

- Synchrotron radio emission from SNRs      **GeV electron**
- $\gamma^0$  decay  $\gamma$ -rays from several SNRs by EGRET      **GeV proton**  
(Esposito et al. 1996)
- Synchrotron X-rays from several SNRs (SN1006, RXJ1713,...)  
(Koyama et al. 1995; Koyama et al. 1997, etc.)      **TeV electron**

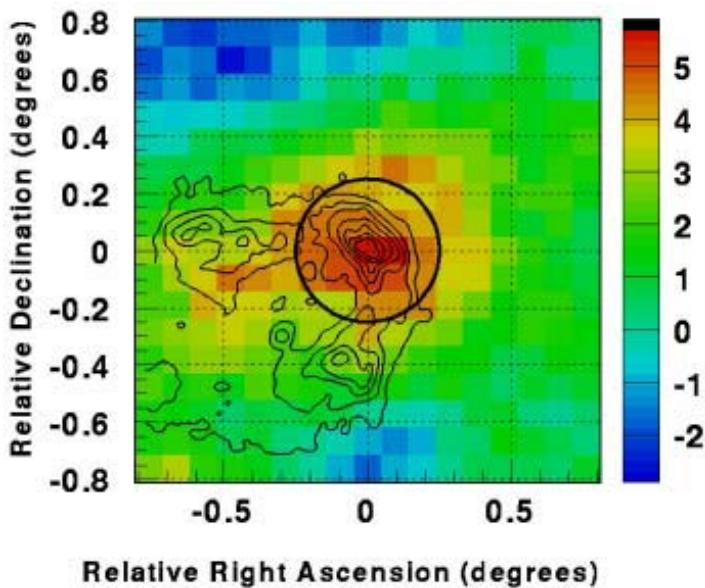
## Most direct evidence

- TeV  $\gamma$ -rays from three SNR have been detected !!

- (1) SN1006 (by CANGAROO)** : **TeV electron**  
(Tanimori et al. 1998)
- (2) RX J1713.7-3926 (by CANGAROO)** : **TeV electron or proton?**  
(Muraishi et al. 2000; Enomoto et al. 2002)
- (3) Cas A (by HEGRA)** : **TeV proton?**

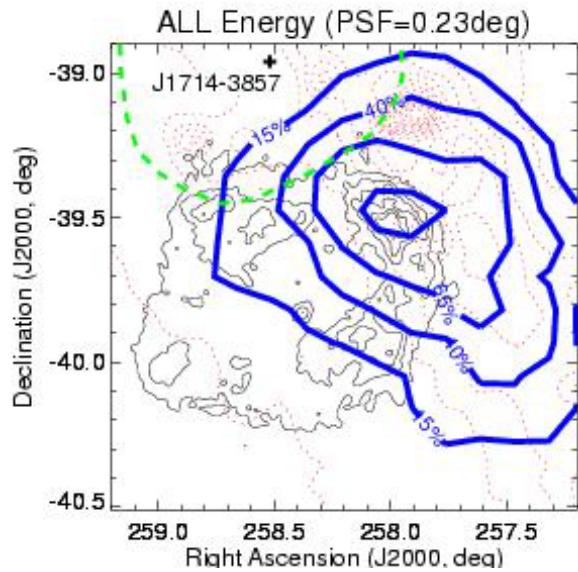
Clear evidence for proton acceleration is still lacked.  
New synchrotron X-ray SNRs (RCW86, RXJ0852).  
Stereoscopic Observations will start soon  
by H.E.S.S., CANGAROO-III, VERITAS, and others

## Significance map around RXJ1713 (CANGAROO observation)



3.8m telescope

Muraishi et al., A&A 357, L57 (2000)



10m telescope

Enomoto et al., Nature 416, 823 (2002)

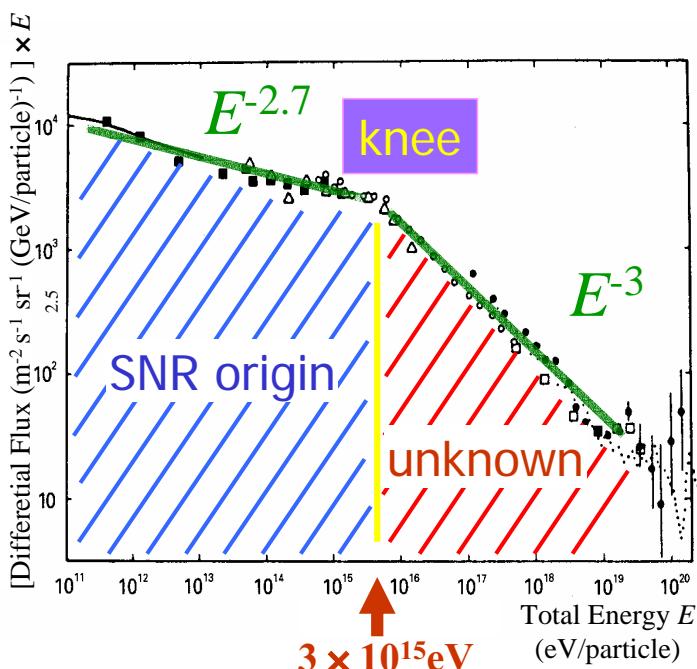
# Possible origin of CRs between $10^{15}$ and $10^{18}$ eV

- (1) Escape from the Galaxy of more energetic particles  
(Peters 1960)
- (2) Z dependence of the maximum energy in shock acceleration  
(Drury 1983, Lagage & Cesarsky 1983)
- (3) Reacceleration of GCRs  
(Jokipii & Morfill 1985)
- (4) Change of the interaction models in EAS  
(Erlykin & Wolfendale 2000)
- (5) Necessity of anomalous (extragalactic) CRs ??  
(Fichtel & Linsley 1986)

## 2. Galactic modulation of extragalactic CRs

### Motivation

#### -Possible existence of V.H.E. CRs in IGS -



CRs in intra-cluster medium (ICM)

◇ EUV and hard X-ray emissions from ICM (Ensslin et al. 1999)

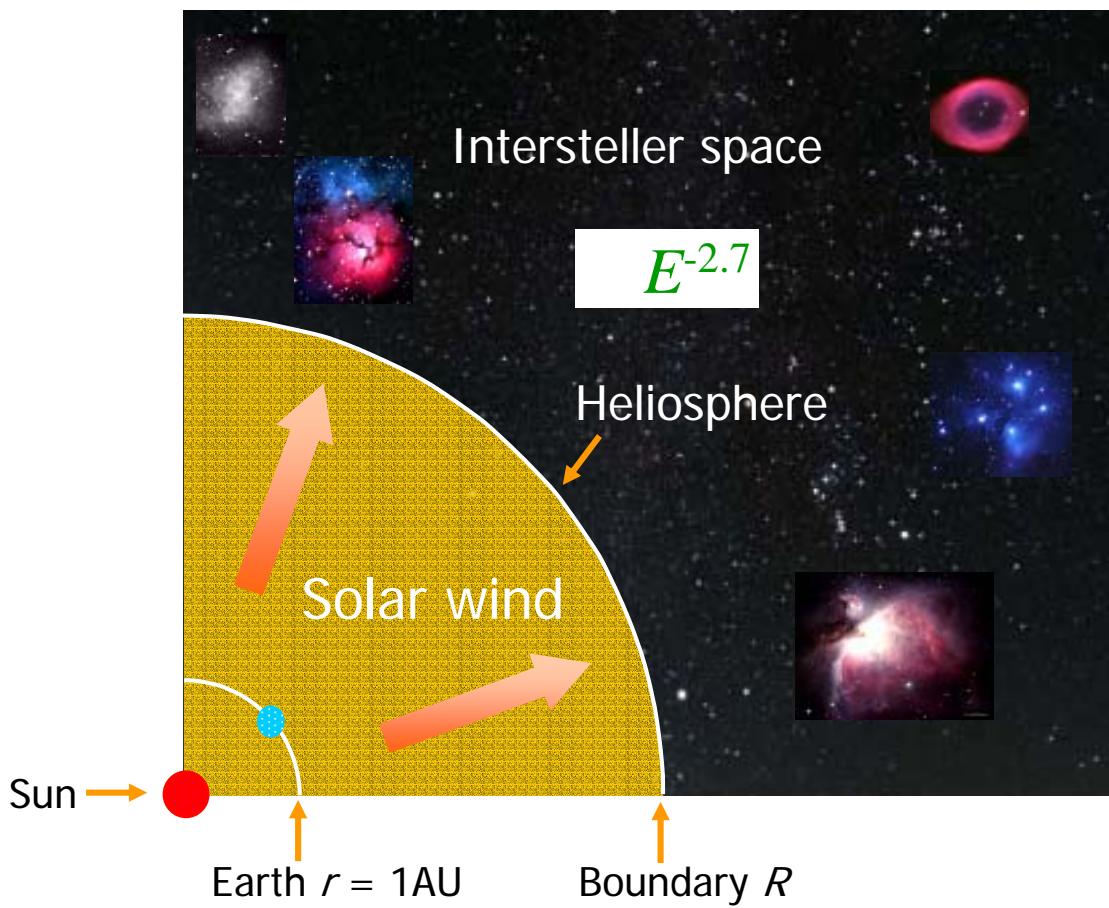
◇ Isotropic extragalactic -ray background (Loeb & Waxman 2000)

**Existence of L.E. CR electron**

If nuclear components with energy up to  $10^{18}$  eV also exist around our Galaxy,

these components modulated by the galactic wind might be directly observable !!!

## Solar modulation



### — Fokker-Plank Eq.(spherical symmetry) — (Parker 1965)

$$\frac{\partial f}{\partial t} = \frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 \kappa \frac{\partial f}{\partial r} \right) - V \frac{\partial f}{\partial r} + \frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 V \right) \frac{p}{3} \frac{\partial f}{\partial p}$$

$t$ : time                           $r$ : radial distance

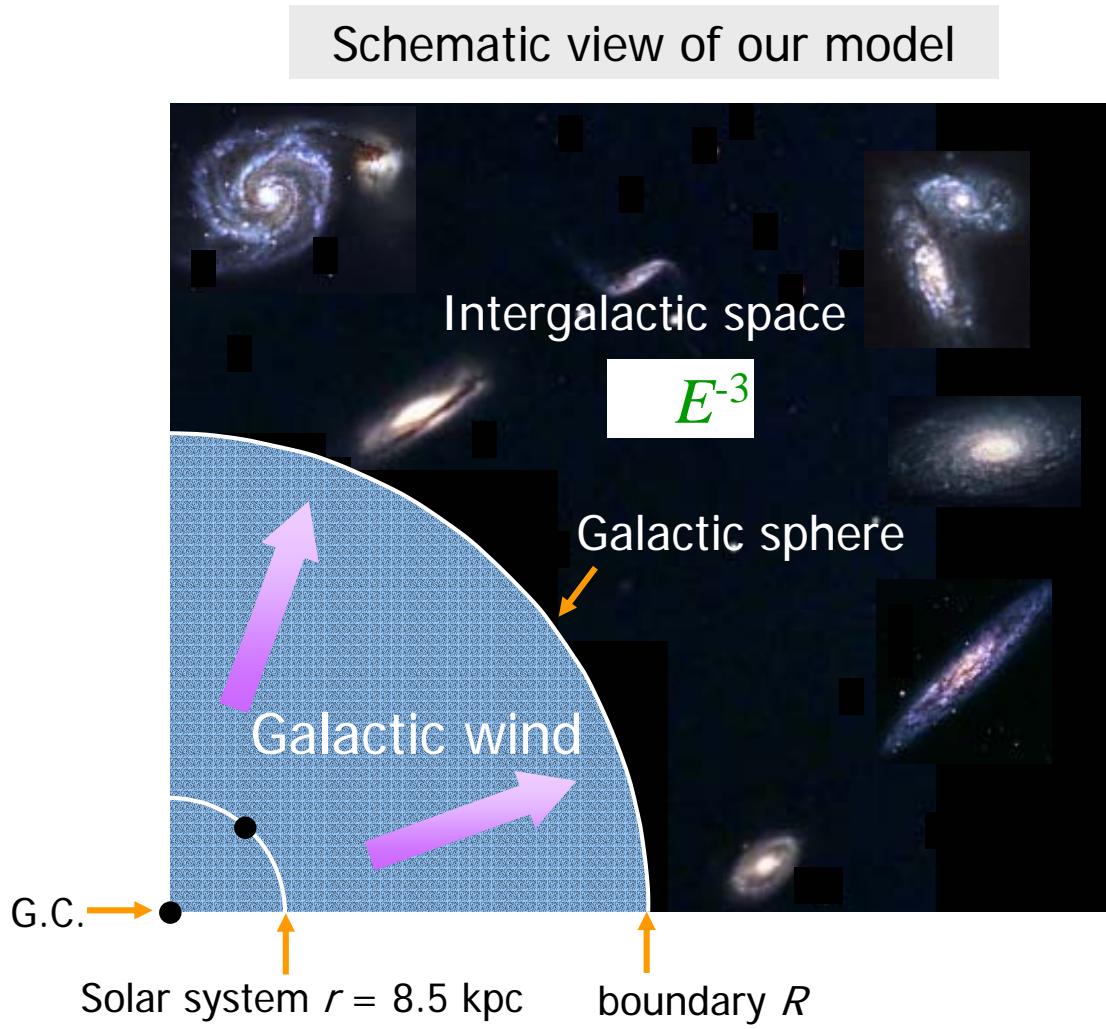
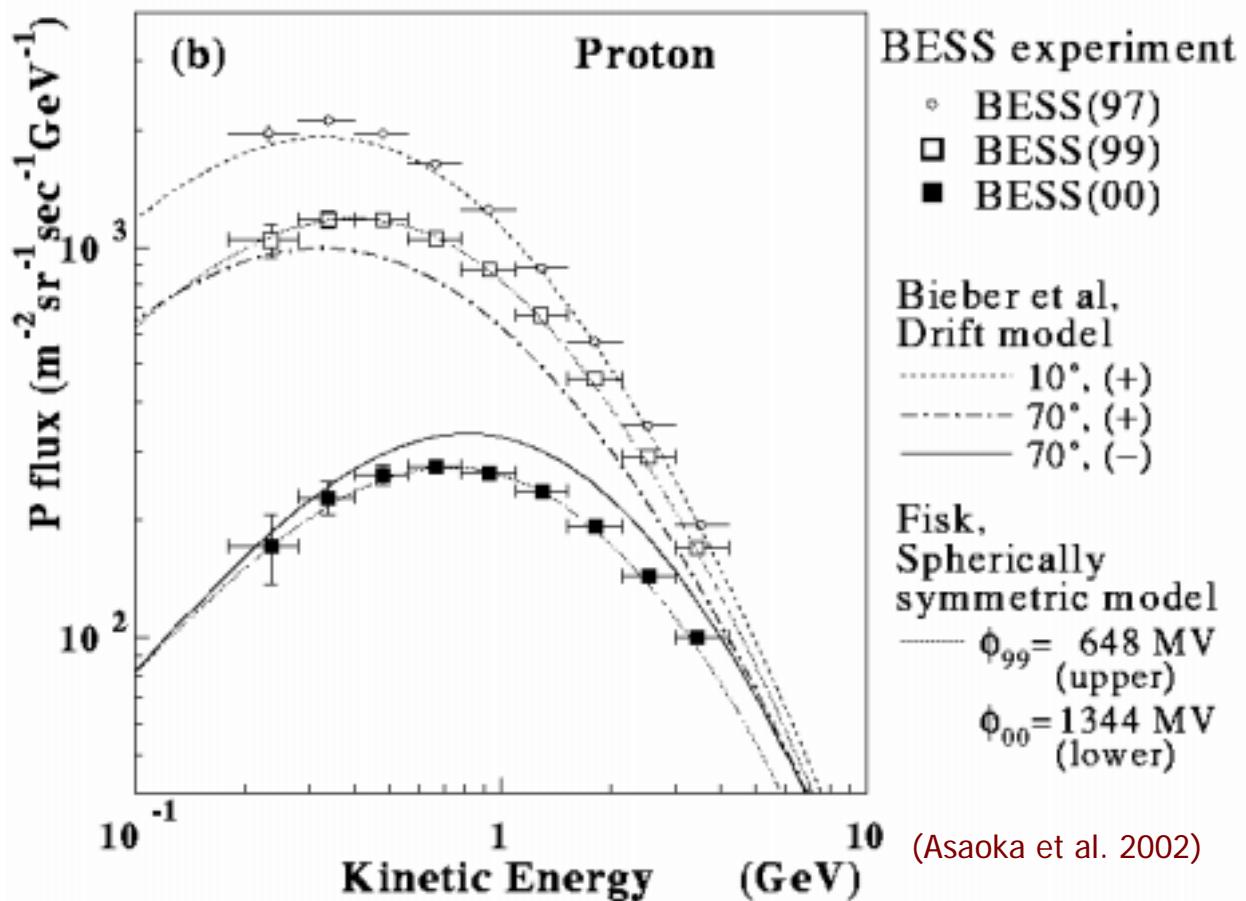
$f$ : distribution function     $V$ : speed of the galactic wind

$p$ : particle momentum     $\kappa$ : diffusion coefficient

### — SDEs equivalent to F-P eq. — (Yamada, Yanagita & Yoshida 1998)

$$\begin{cases} dr = \left( V + \frac{2\kappa}{r} + \frac{\partial \kappa}{\partial r} \right) dt + \sqrt{2\kappa} dw \\ du = -\frac{2V}{3r} dt \quad (u \equiv \ln(p/mc)) \end{cases}$$

$dw$ : Wiener process given by a Gaussian distribution



## diffusion coefficient

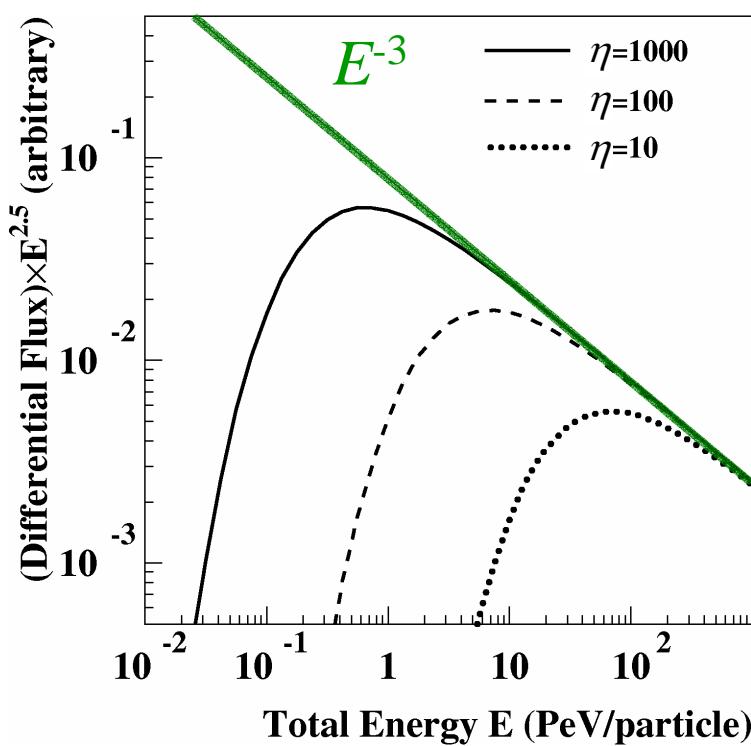
$$\kappa = \eta \kappa_{\text{Bohm}} \approx 3.3 \times 10^{28} \eta Z^{-1} \left( \frac{E}{1 \text{PeV}} \right) \left( \frac{B}{1 \mu\text{G}} \right)^{-1} \text{cm}^2 \text{s}^{-1}$$

$\kappa_{\text{Bohm}}$  : Bohm diffusion coefficient

$\eta$  : the ratio of diffusion mean free path to Larmor radius

$B$  : magnetic field in the Galactic halo

## Modulated spectra of protons near at the earth ( $r=8.5\text{kpc}$ )



- radial distance of the galactic sphere:

$$R = 100 \text{kpc}$$

(Zirakashvili et al. 1996)

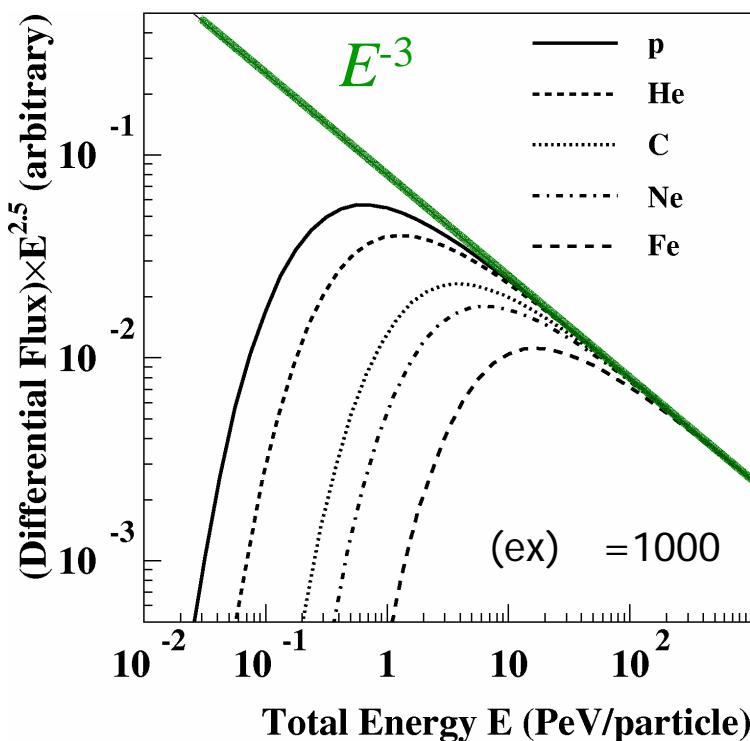
- speed of the galactic wind:

$$V = 300 \text{ km s}^{-1}$$

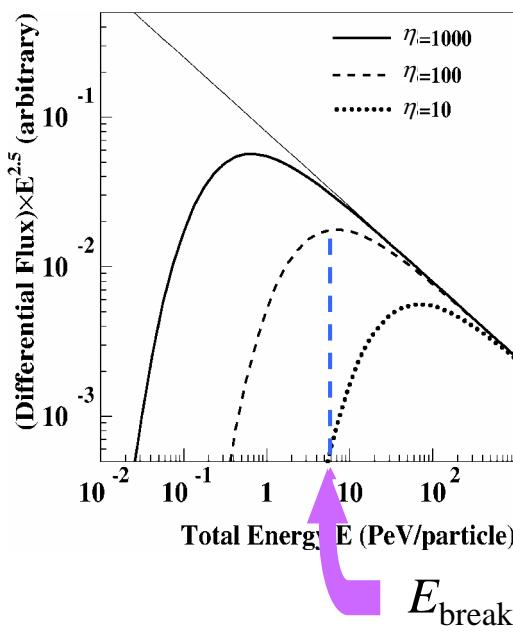
- magnetic field:

$$B = 1 \mu\text{G}$$

# Modulated spectra of various nuclear components



Break point in the modulated spectrum of the hypothetical extragalactic CRs



$$E_{\text{break}}(\eta, B, R, V, Z) \approx 6 \times 10^{15} Z \left( \frac{\eta}{100} \right)^{-1} \left( \frac{B}{1 \mu\text{G}} \right) \left( \frac{R}{100 \text{kpc}} \right) \left( \frac{V}{300 \text{ km s}^{-1}} \right) \text{ eV}$$

### 3. A model of the all-particle spectrum near the knee region

$$F_{\text{Total}}(E) = F_{\text{Modul}}(E) + F_{\text{SNR}}(E)$$

$F_{\text{Total}}$  : expected all-particle spectrum

$F_{\text{Modul}}$  : modulated spectrum of the hypothetical extragalactic CRs

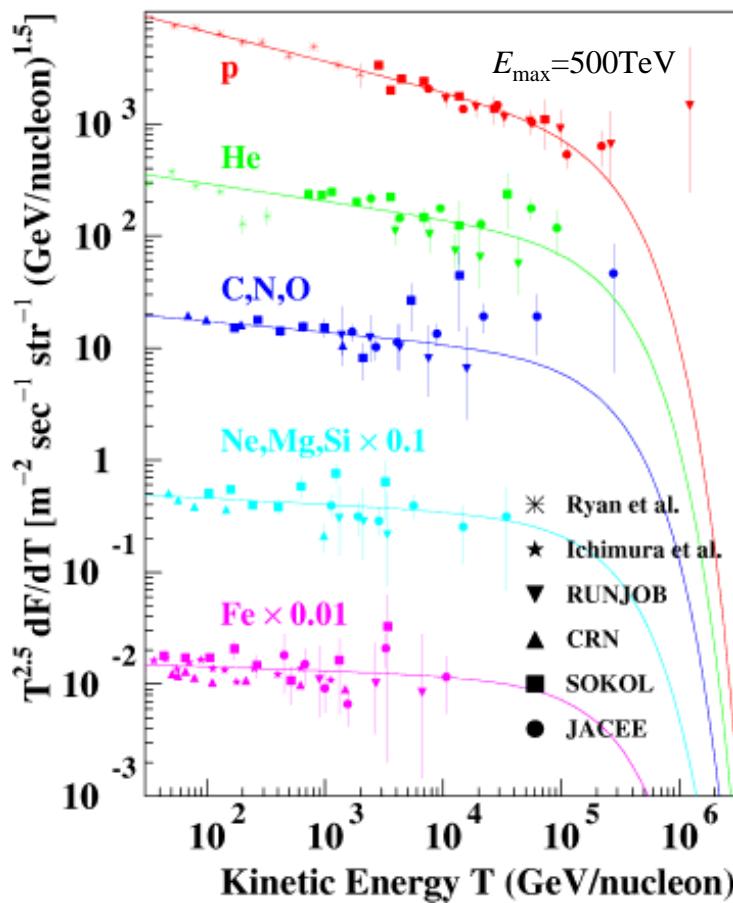
$F_{\text{SNR}}$  : all-particle spectrum of the GCRs from SNRs

$$F_{\text{SNR}}(E) = \sum_Z f_z(E)$$
$$f_z(E) \propto E^{-\alpha} \exp(-E/(ZE_{\text{max}}))$$

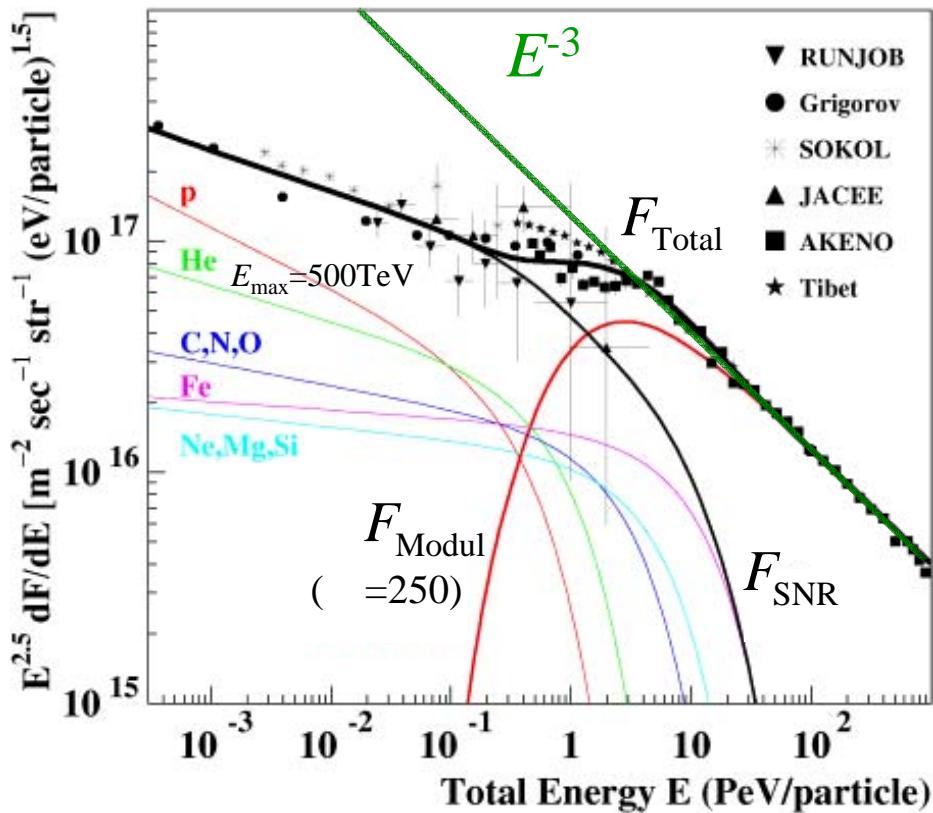
$Z$  : atomic number

$E_{\text{max}}$  : maximum energy attained by protons in SNRs

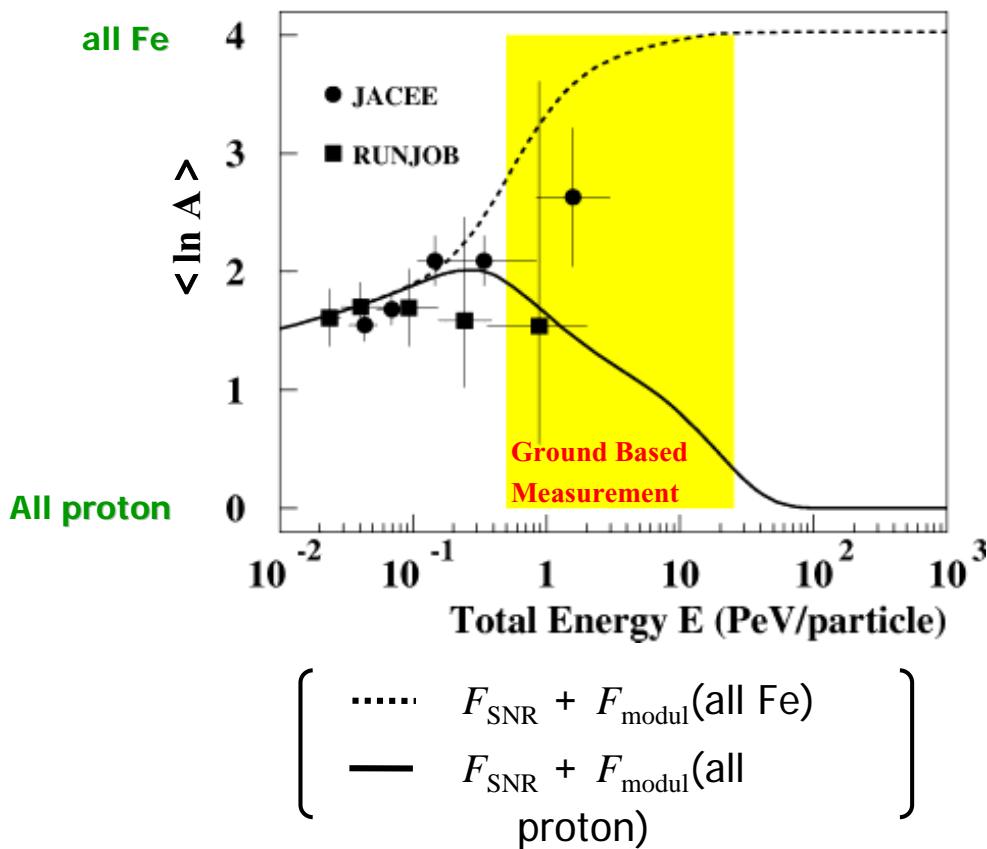
### Energy spectra of GCRs and the fitted curves



## Comparison of the model spectrum with the observations



## Expected mean mass of CRs around the knee region



# 4. Discussion

## ✧ Energetics of the hypothetical CRs

### Upper limit

- Energy spectrum of the hypothetical CRs at the boundary of the galactic sphere

$$F_{\text{CR}}(E) \approx 4.3 \times 10^{20} E^{-3} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \text{ eV}^{-1}$$

$$\longrightarrow \rho_{\text{CR}} = \int_{E_m}^{\infty} \frac{4\pi}{v} F_{\text{CR}}(E) E dE \approx 294 \text{ eV cm}^{-3}$$

- Corresponding density parameter

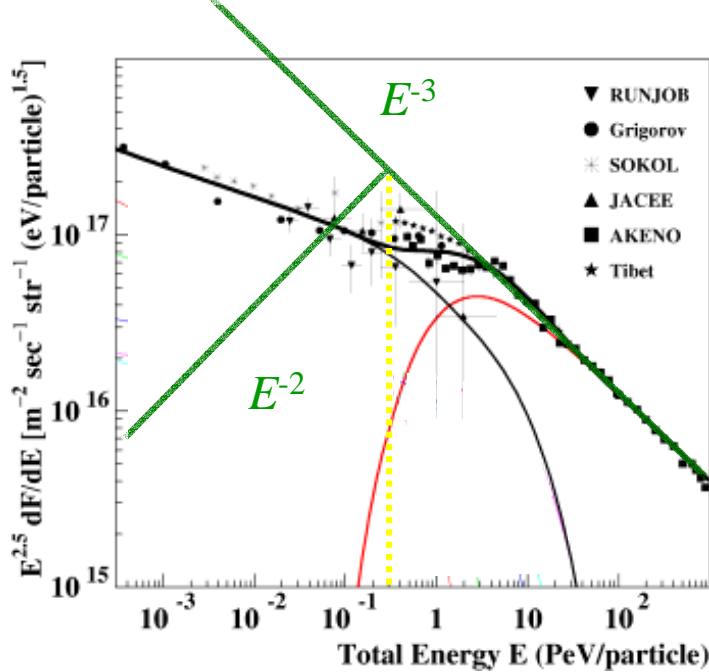
$$\Omega_{\text{CR}} h_{70}^2 \approx 0.057 \quad (\sim \Omega_B h_{70}^2 \approx 0.041)$$

(Burles et al. 2001)

The spectrum becomes harder in the energy lower than the knee and/or CRs are confined in local regions

Contribution of CRs to Dark Matter ??

### Lower limit



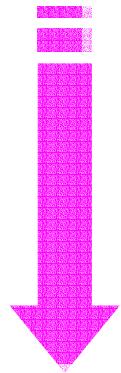
If  $F_{\text{CR}}(E) \approx \begin{cases} 4.3 \times 10^{20} E^{-3} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \text{ eV}^{-1} & (\geq 10^{14.5} \text{ eV}) \\ 1.3 \times 10^6 E^{-2} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \text{ eV}^{-1} & (\leq 10^{14.5} \text{ eV}) \end{cases}$

$$\longrightarrow \rho_{\text{CR}} = \int_{E_m}^{\infty} \frac{4\pi}{v} F_{\text{CR}}(E) E dE \approx 0.0078 \text{ eV cm}^{-3}$$

**much small !**

## ✧ Origin of the hypothetical extragalactic CRs

- Reacceleration of GCRs ? (Jokipii & Morfill 1985)
- Early starburst ? (Voelk & Atoyan 2000)
- Cluster merger ? (Blasi 2001)
- Shock acceleration in large-scale structure formation ?  
(Mati et al. 2000)



More energetic !

## ✧ Search for hypothetical extragalactic CRs

### Recently

- Association of galaxy clusters with EGRET unidentified -ray sources (Totani & Kitayama 2000, Colofrancesco 2002)  
**Evidence for the existence of extragalactic GeV CRs ?**

### In the future

- PeV -ray observation from SMC  
**search for the extragalactic PeV CRs???**
- CANGAROOIII observation from cluster merger  
**search for the extragalactic TeV CRs???**  
**(ex) A violent cluster merger Abell3376**

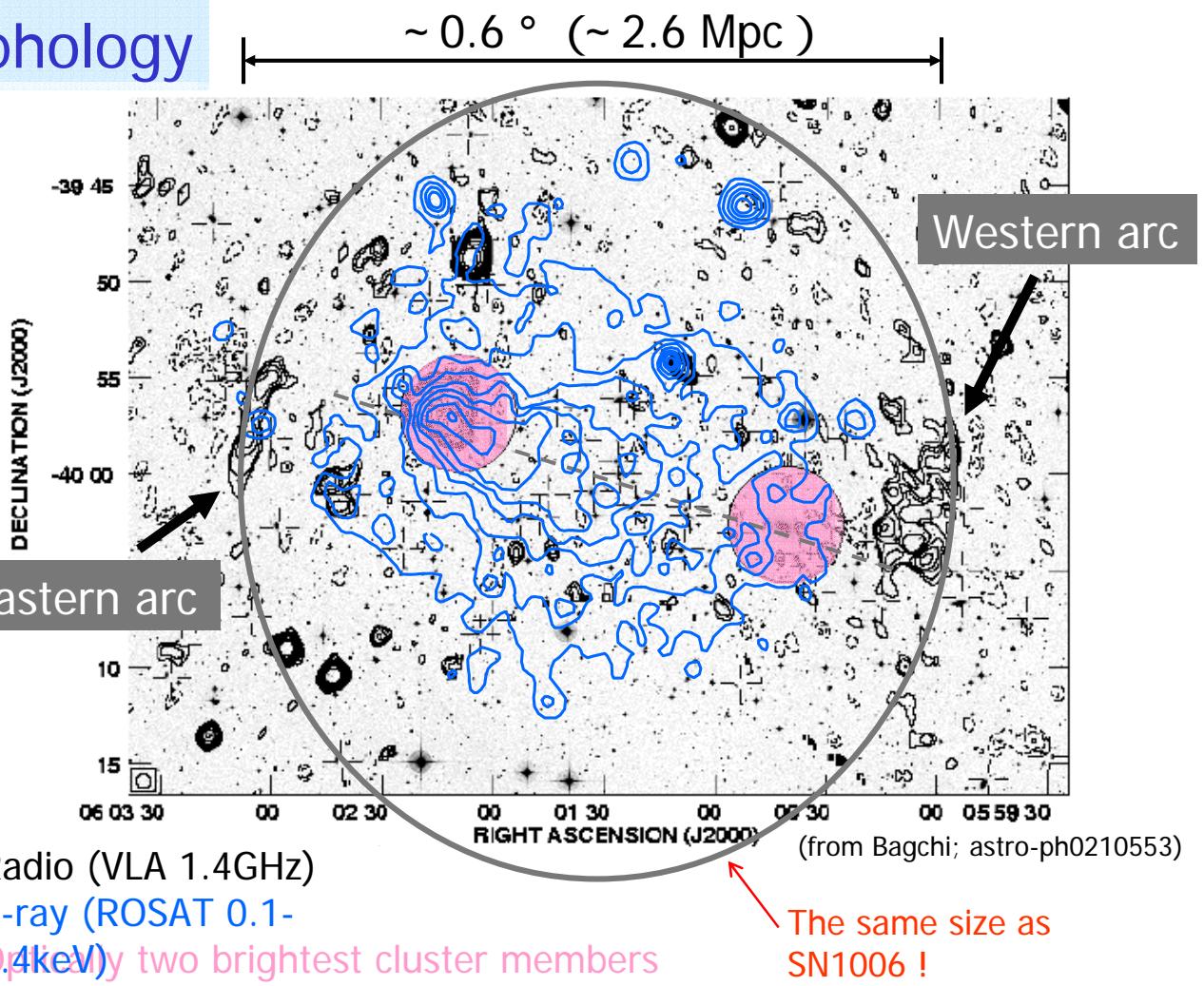
# Introduction of Abell 3376

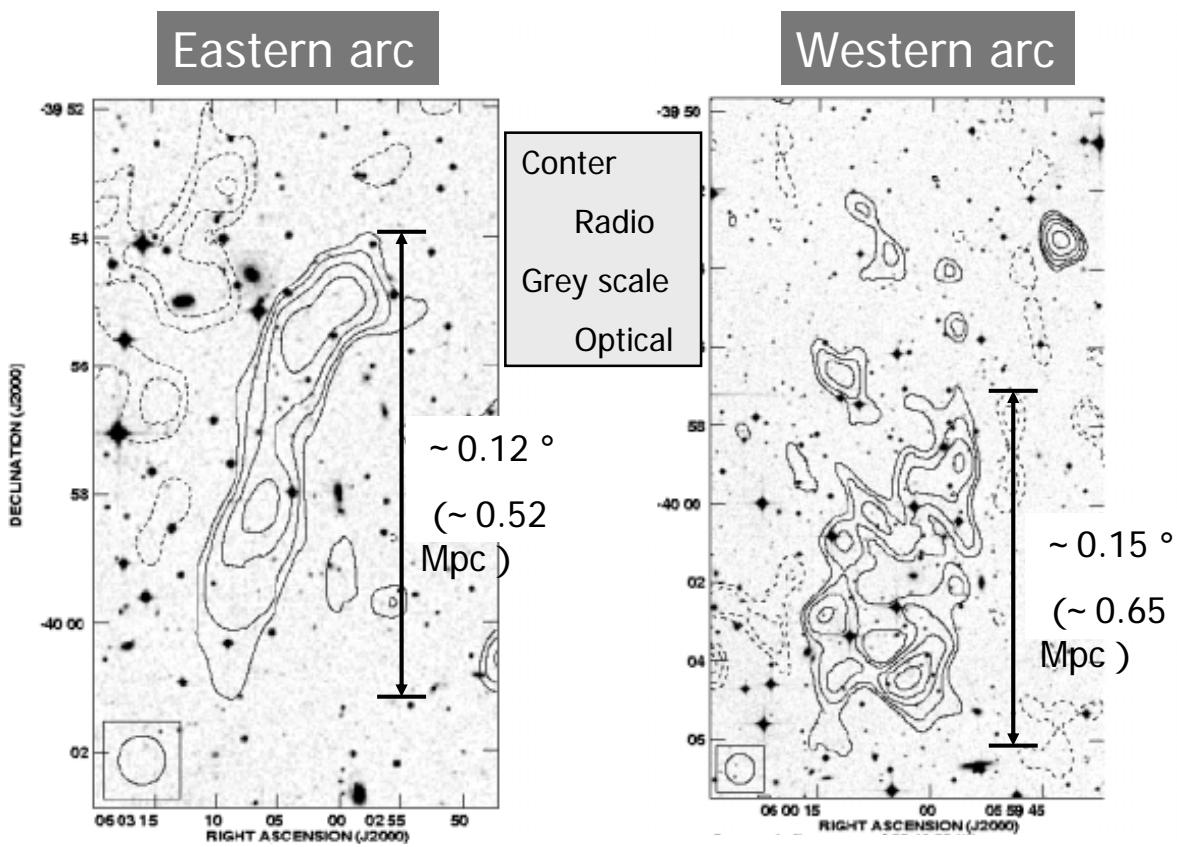
- Cluster of Galaxy
- Evidence for cluster merger (radio, optical, X-ray)
- $Z=0.046$  (200 Mpc)
- No EGRET un-ID source around Abell3376

- Discovery of giant 'synchrotron radio arcs'  
(Bagchi; astro-ph/0210553 , submitted to MNRAS 2002)  
Existence of Mpc scale shock-waves, which occur  
during cluster formation

Very interesting !

## Morphology





Optically no counter part exist around the arcs.

**Synchrotron radio emission!**

**Evidence for Mpc scale shock-waves, which occur during cluster formation**

## Maximum energy in the arcs

Accerelation time for diffusive shock acceleration (Drury 1983)

$$t_{\text{acc}} = \frac{r_c(r_c - 1)}{r_c - 1} \frac{Ec}{eBv_{\text{shock}}}$$

$E$  : particle energy     $v_{\text{shock}}$  : shock velocity

$B$  : magnetic field strength in the arcs

$r_c$  : compression ratio (=4 for strong shock)

By assuming the Bohm diffusion,

For proton : if  $t_{\text{acc}} \leq t_{\text{merger}} \approx 10^9 \left( \frac{d}{1.8 \text{Mpc}} \right) \left( \frac{v_{\text{shock}}}{2000 \text{ km s}^{-1}} \right)^{-1} \text{ yr}$  then

$$E_{\text{max}}^{\text{proton}} \leq 4.8 \times 10^{18} \left( \frac{B}{1 \mu\text{G}} \right) \left( \frac{v_{\text{shock}}}{2000 \text{ km s}^{-1}} \right)^2 \text{ eV}$$

**Origin of UHECR ?**

For electron : if  $t_{\text{acc}} \leq t_{\text{radiation (IC)}} \leq t_{\text{merger}}$  then

$$E_{\text{max}}^{\text{electron}} \leq 7.4 \times 10^{13} \left( \frac{B}{1 \mu\text{G}} \right)^{0.5} \left( \frac{v_{\text{shock}}}{2000 \text{ km s}^{-1}} \right) \text{ eV}$$

**Possible to emit  
subTeV-TeV  
rays by IC !**

# Detectability of TeV -rays from the arcs ~Analogy with the results for SN1006~

## Relation between synchrotron and IC losses

$$\frac{F_{\text{syn}}}{F_{\text{IC}}} = \frac{U_B}{U_{\text{ph}}} \quad F_{\text{syn}} : \text{Synchrotron flux} \quad U_{\text{ph}} : \text{Photon density (CMB)}$$

$$F_{\text{IC}} : \text{IC flux} \quad U_B : \text{Magnetic energy density}$$

$(= B^2 / 8\pi)$

Radio flux from the arcs in A3376

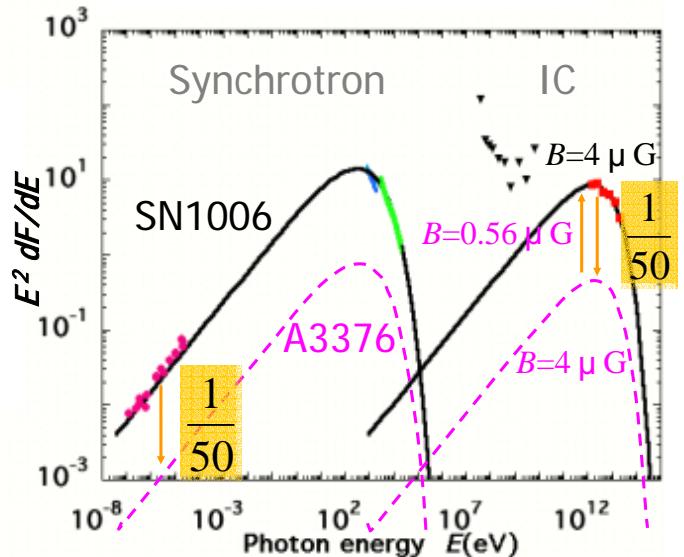
1/50 smaller than that for  
SN1006 NE-rim

To get the same TeV flux as 1006

$$B_{\text{Abell3376}} = \sqrt{\frac{1}{50}} B_{\text{SN1006}} = \underline{0.56 \mu\text{G}}$$

$(\because B_{\text{SN1006}} = 4 \mu\text{G})$

It's a reasonable value in the arcs



## Energetics

✧ Power supply by cluster merger

$$P_G \approx \frac{E_G}{t_{\text{merger}}} = 2 \times 10^{47} \left( \frac{M}{2 \times 10^{14} M_\bullet} \right) \left( \frac{d}{1.8 \text{Mpc}} \right)^{-2} \left( \frac{v_{\text{shock}}}{2000 \text{km s}^{-1}} \right)^{-1} \text{erg s}^{-1}$$

✧ Emissivity of TeV -rays by IC

If  $F(>1\text{TeV}) \approx 10^{-11} \text{ erg cm}^{-2} \text{s}^{-1}$ ,

$$\longrightarrow P_{\text{TeV}} \approx 4\pi r^2 \times F = 4 \times 10^{44} \left( \frac{r}{200 \text{Mpc}} \right)^2 \text{erg s}^{-1}$$

$P_G \sim 0.002 P_{\text{TeV}}$

Possible to detect TeV -rays from  
Abell3376 !

## Motivation of CANGAROO observation from the cluster merger Abell3376

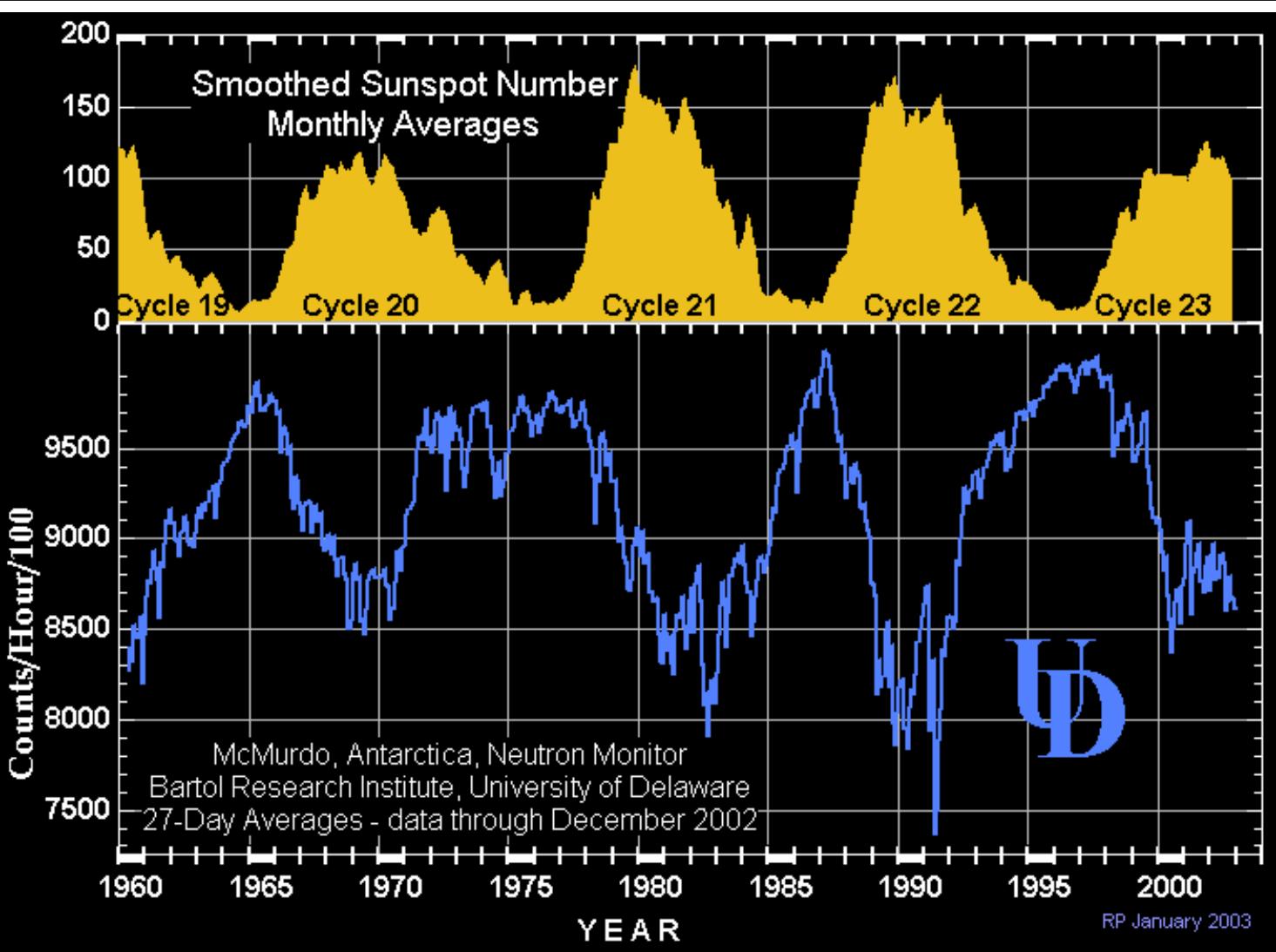
- Evidence for Diffusive shock acceleration in Cosmic shock
- Discovery of the Existence of high energy CRs in the intracluster space
- Search for the origin of HE. or UHECRs in cosmic shock
- New source in TeV  $\gamma$ -ray astronomy

## 5. Conclusion

- All-particle spectrum of CRs around “the knee” region is reproduced well by a superposition of the two components,  
  
*GCRs of SNR origin and,  
the extragalactic CRs modulated by the galactic wind.*
- The position of “the knee” may give us ideas on the structure of the galactic sphere (its size, the speed of the galactic wind, and etc. etc.) .
- Future observations of CRs above the knee region will tell us the chemical composition of the extragalactic CRs.
- Simulation experiments in more realistic setting for galactic structure are needed.

-The END-

# 補足



# Dependence of modulated spectra on the diffusion coefficient

