

# ***Theoretical Impact of Neutrinoless Double Beta Decay Experiments***

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# 1 Introduction

## Neutrinos: Windows to New Physics

**Neutrino Oscillations provided information**

- **Tiny Neutrino Masses**
- **Large Neutrino Flavor Mixings**

**Flavor Symmetry, Extra Dimensions . . . .**

**Connecting Physical Phenomena**

**Neutrinoless Double Beta Decay**

**Leptogenesis . . . . .**

# Questions

★ Tiny Neutrino Masses ?    Seesaw, Extra-Dimensions

★ Large Flavor Mixings ?    Flavor symmetry

★ Majorana Neutrinos ?    ( L number violation? )

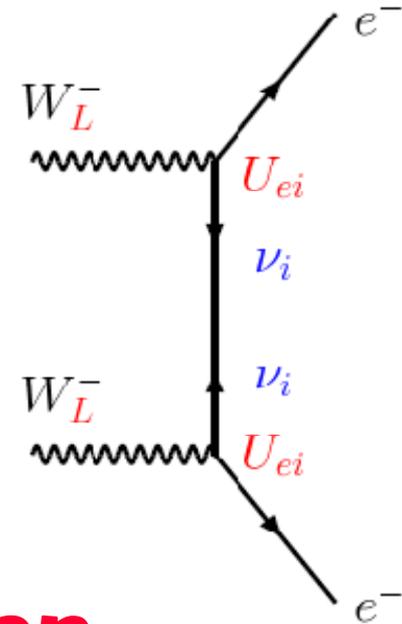
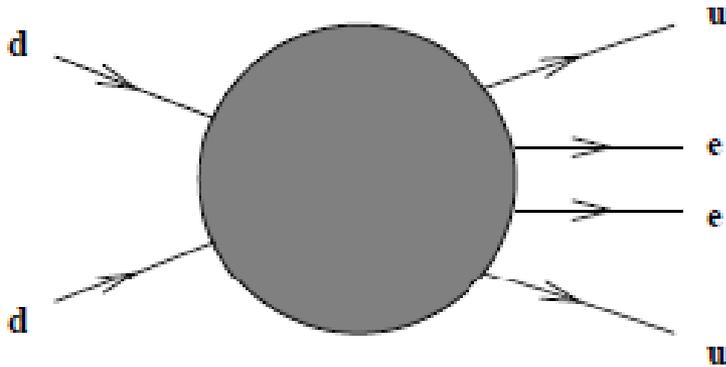
★ Right-handed Neutrinos ?

★ Sterile Neutrinos ?

★ New Interaction of Neutrinos ?

★ Neutrino Soft Mass ?

## 2 Neutrinoless Double Beta Decay



**Majorana Neutrino**

**Lepton Number Violation**

**Baryon Asymmetry can be explained by Leptogenesis due to violation of  $(B - L)$**

$$\frac{1}{T_{1/2}} = G^{0\nu}(E_0, Z) |M^{0\nu}|^2 |\langle m_\nu \rangle|^2$$

$G^{0\nu}$  : phase space factor

$M^{0\nu}$  : nuclear matrix element

**Still  
Uncertainties**

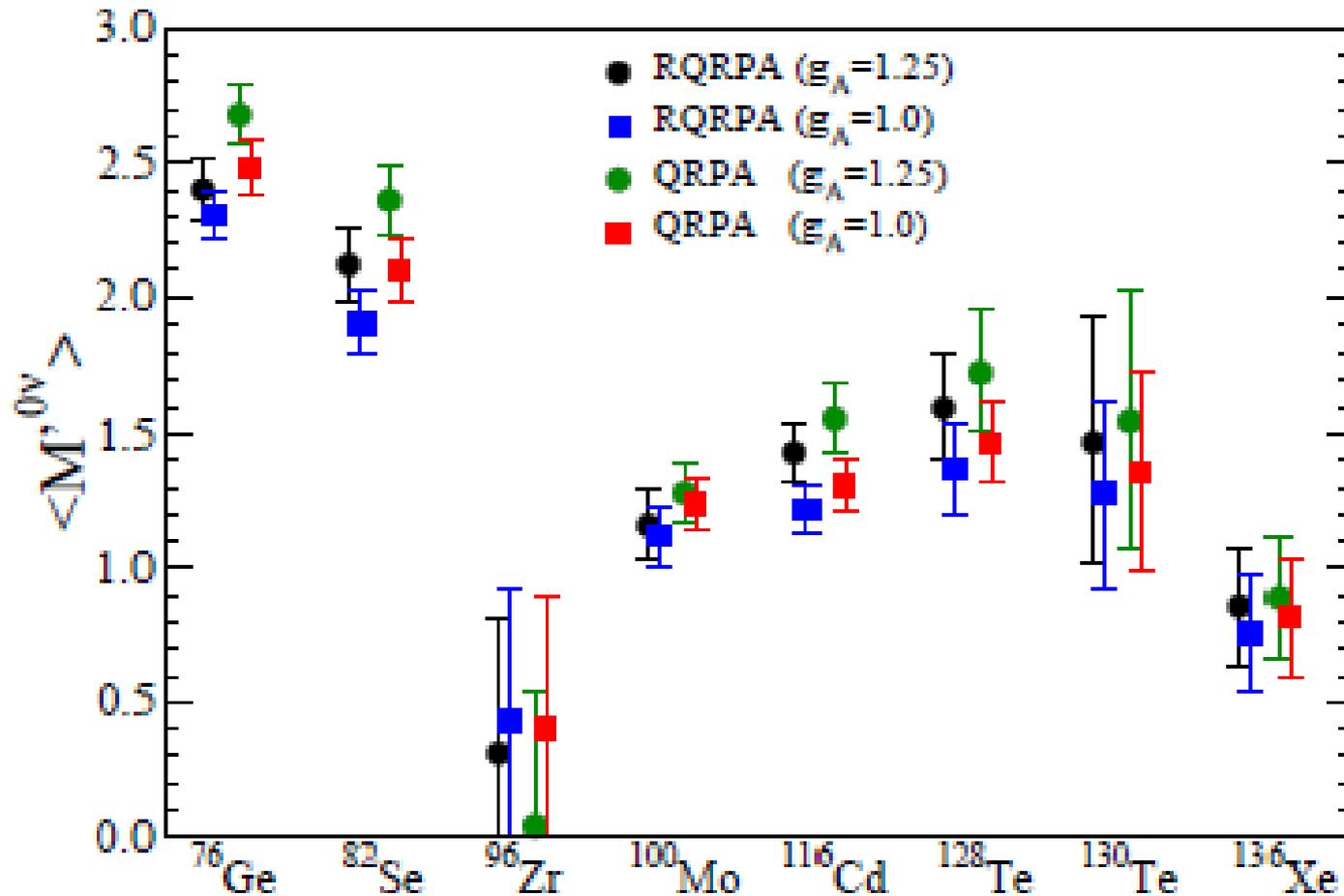
$$\langle m_\nu \rangle = \left| \sum_i^3 U_{ei}^2 e^{i\alpha_i} m_i \right|$$

$$= |\mathbf{M}_\nu(\mathbf{1}, \mathbf{1})|$$

$$\langle m_\nu \rangle = c_{12}^2 m_1 + s_{12}^2 c_{13}^2 e^{i\alpha_1} m_2 + s_{13}^2 e^{i\alpha_2} m_3$$

**The magnitude depends on neutrino mass hierarchy.**

**Generally,  $\langle m_\nu \rangle$  is large in the case of inverted masses  $m_2, m_1 \gg m_3$ .**



**Rodin, Simkovic, Faessler, Vogel, Nucl. Phys. A766(2006)107**

# Best Present Bound

$$\langle m_\nu \rangle < 0.35 - 0.50 \text{ eV}$$

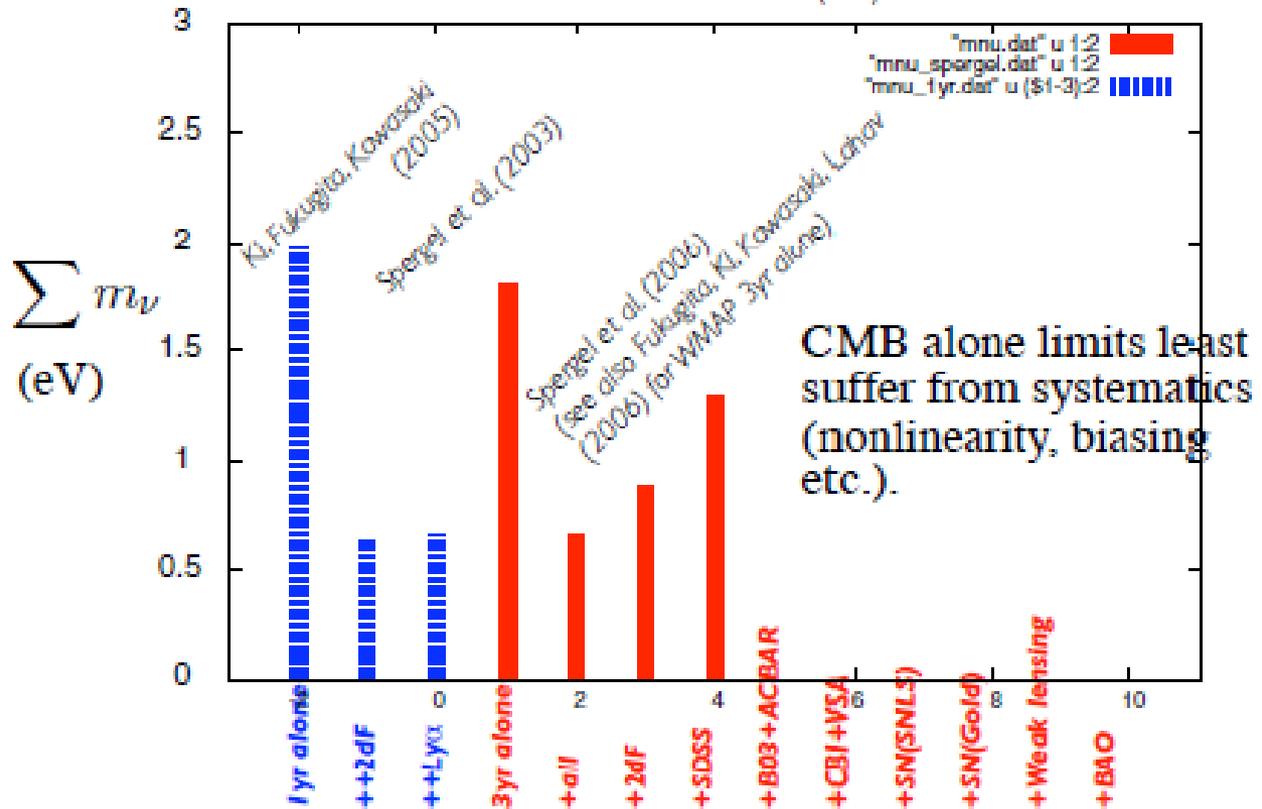


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${}^{76}\text{Ge}$  half-life of  $T_{1/2} > 1.2 \times 10^{25}$  ys

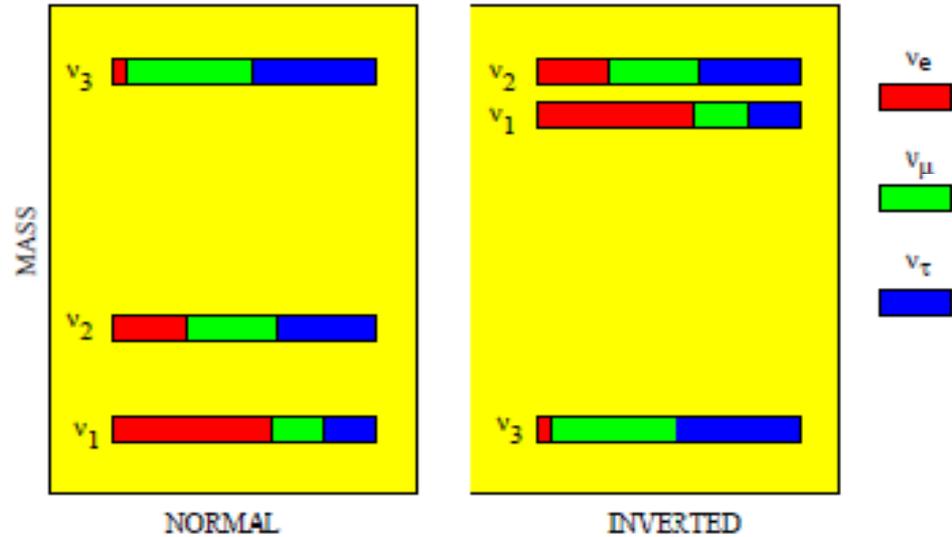
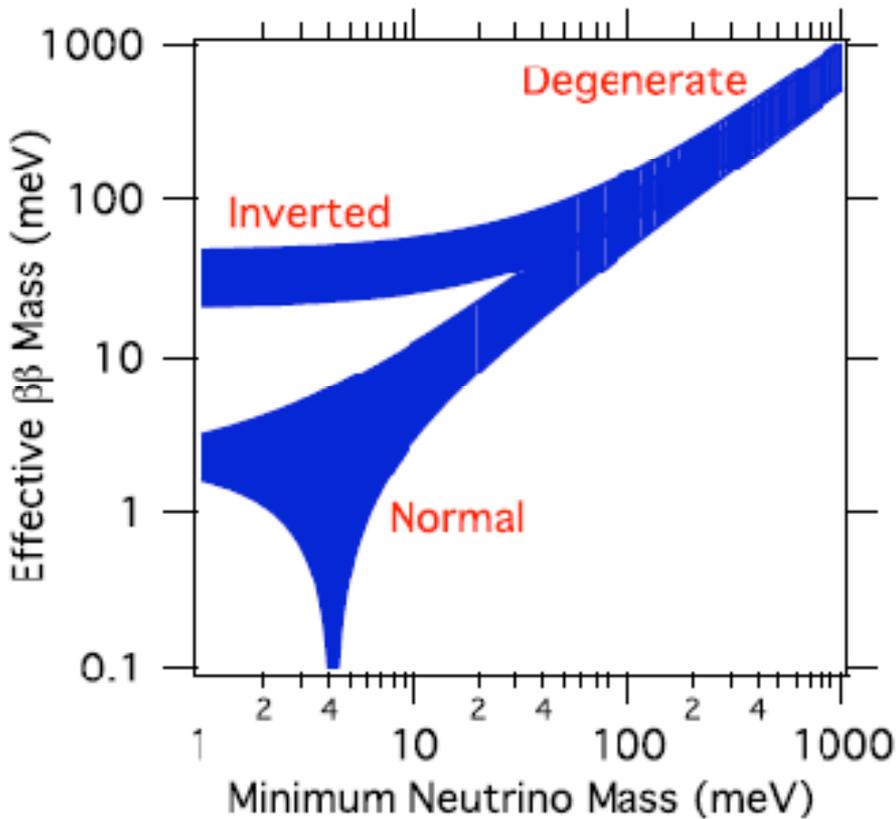
which is consistent with cosmological bound:

Neutrino mass:  $\sum m_\nu < 2.0 \text{ eV}$  (95%)  
mnu constraints/CDM+mnu (95%)



K. Ichikawa  
2006

**Estimate by using best fit values of parameters including uncertainties of Majorana phases.**

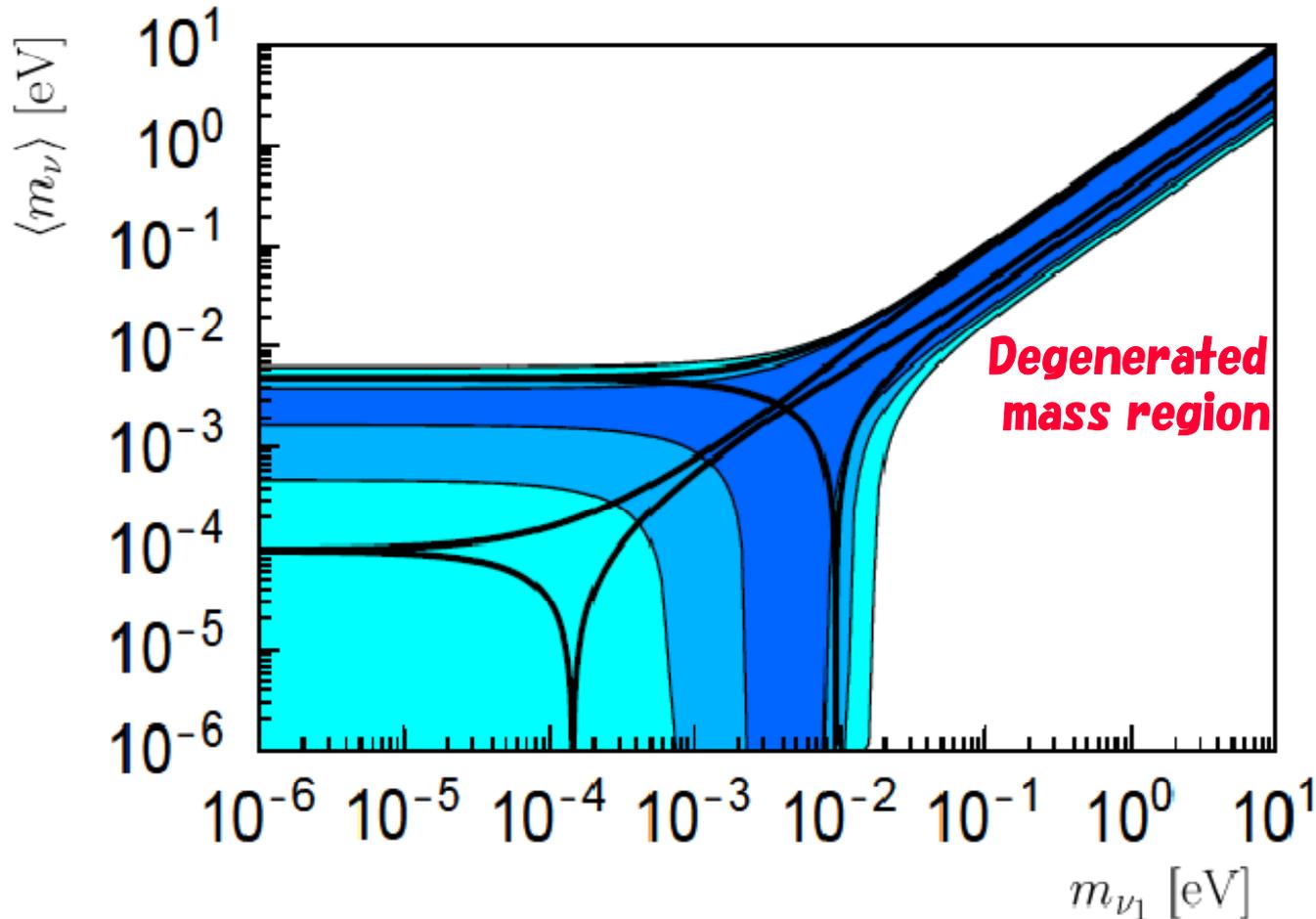


M. Hirsch : [hep-ph/0609146](https://arxiv.org/abs/hep-ph/0609146)

$$m_1 < m_2 < m_3$$

## Normal hierarchy

$$\langle m_\nu \rangle = c_{sun}^2 c_{rea}^2 m_1 + s_{sun}^2 c_{rea}^2 e^{i\alpha_1} \sqrt{m_1^2 + \Delta m_{sun}^2} + s_{rea}^2 e^{i\alpha_2} \sqrt{m_1^2 + \Delta m_{sun}^2 + \Delta m_{atm}^2}$$

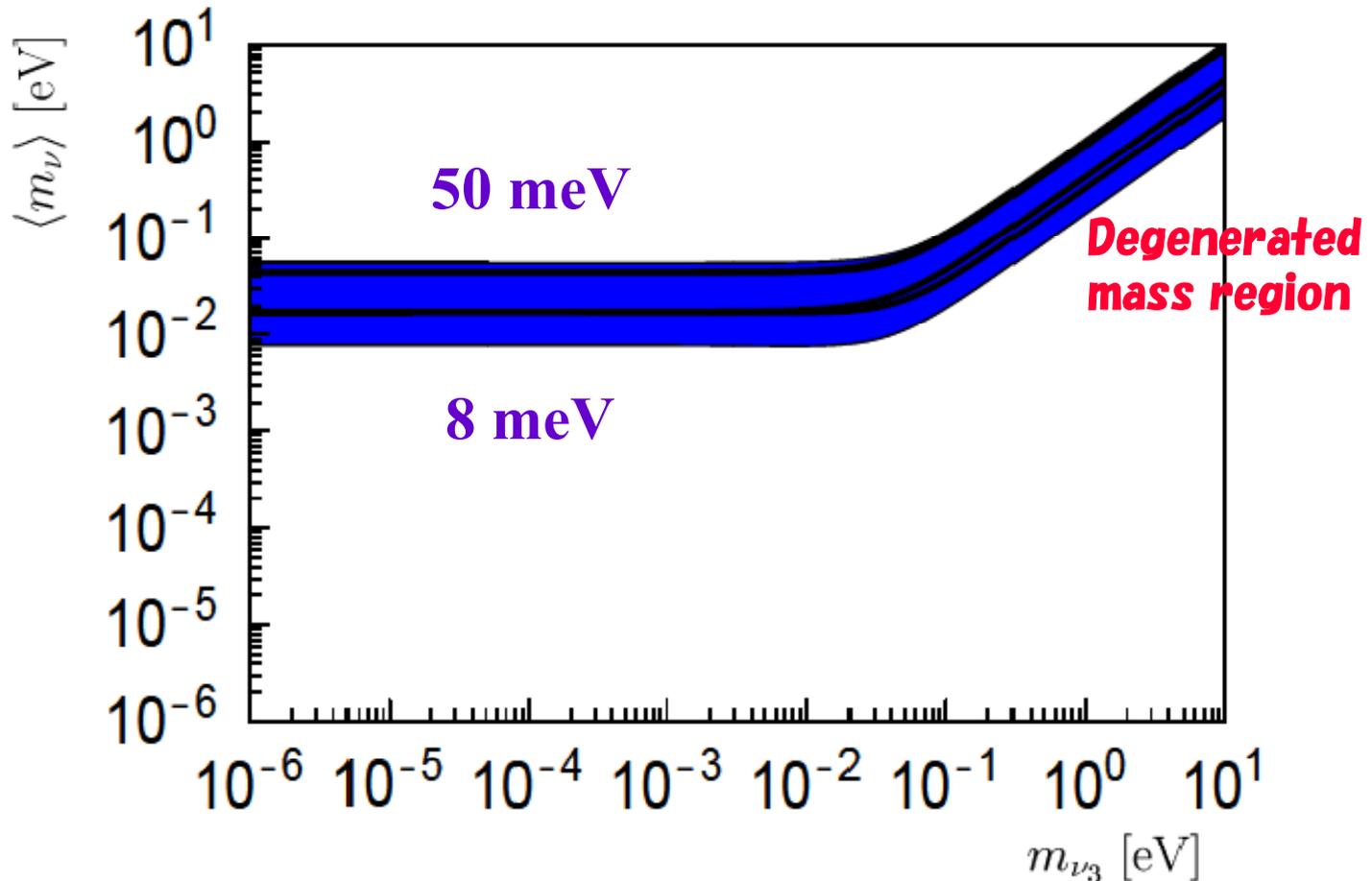


hierarchy, for which 3 different cases for the upper limit on  $s_R^2$  are shown. These are  $s_R^2 \leq 0.04$  (light blue),  $s_R^2 \leq 0.025$  (medium blue),  $s_R^2 \leq 0.005$  (darker blue).

M. Hirsch : [hep-ph/0609146](https://arxiv.org/abs/hep-ph/0609146)  
**Inverted hierarchy**

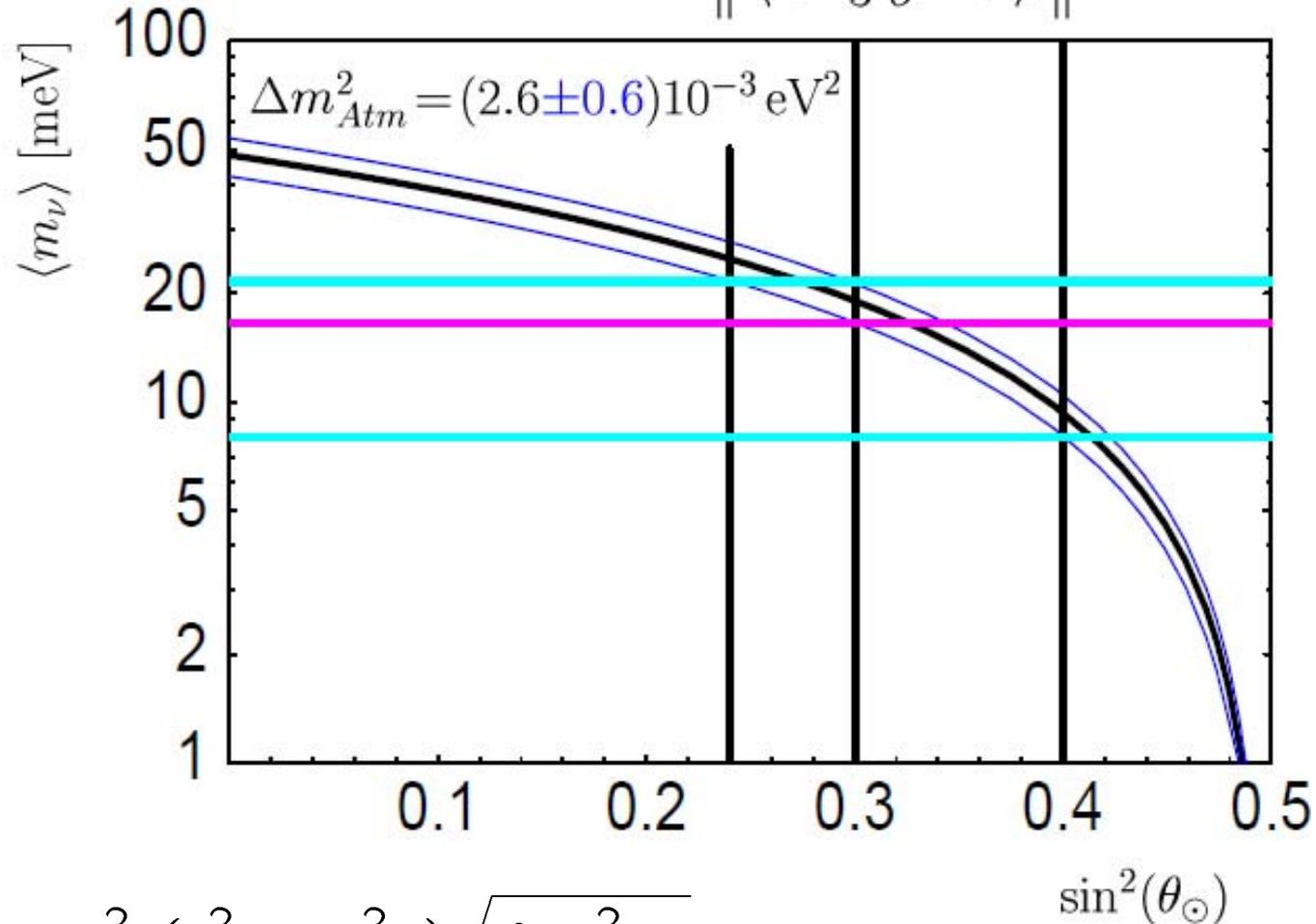
$$m_3 < m_1 < m_2$$

$$\langle m_\nu \rangle = c_{sun}^2 c_{rea}^2 \sqrt{m_3^2 - \Delta m_{sun}^2 + \Delta m_{atm}^2} + s_{sun}^2 c_{rea}^2 e^{i\alpha_1} \sqrt{m_3^2 + \Delta m_{atm}^2} + s_{rea}^2 e^{i\alpha_2} m_3$$



**Lower Limit 8meV**

|| ← 3σ → ||



$$\langle m_\nu \rangle \simeq c_{13}^2 (c_{sol}^2 - s_{sol}^2) \sqrt{\Delta m_{Atm}^2}$$

$\sin^2(\theta_\odot)$

### 3 Neutrino Mass Matrix

**What is the impact on the models of neutrino mass matrix ?**

Since there are a lot of models, it is difficult to distinguish models only by the neutrinoless double beta decay.

**However, models can be tested within the framework of the specific flavor symmetry, for example,  $A_4$  symmetry.**

**Let us show one example !**

# Experimental data favor **Tri-Bi-Maximal mixings.**

Harrison, Perkins, Scott (2002)

$$U_{\text{MNS}} \sim \begin{pmatrix} \sqrt{\frac{2}{3}} & \frac{1}{\sqrt{3}} & 0 \\ -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & -\frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

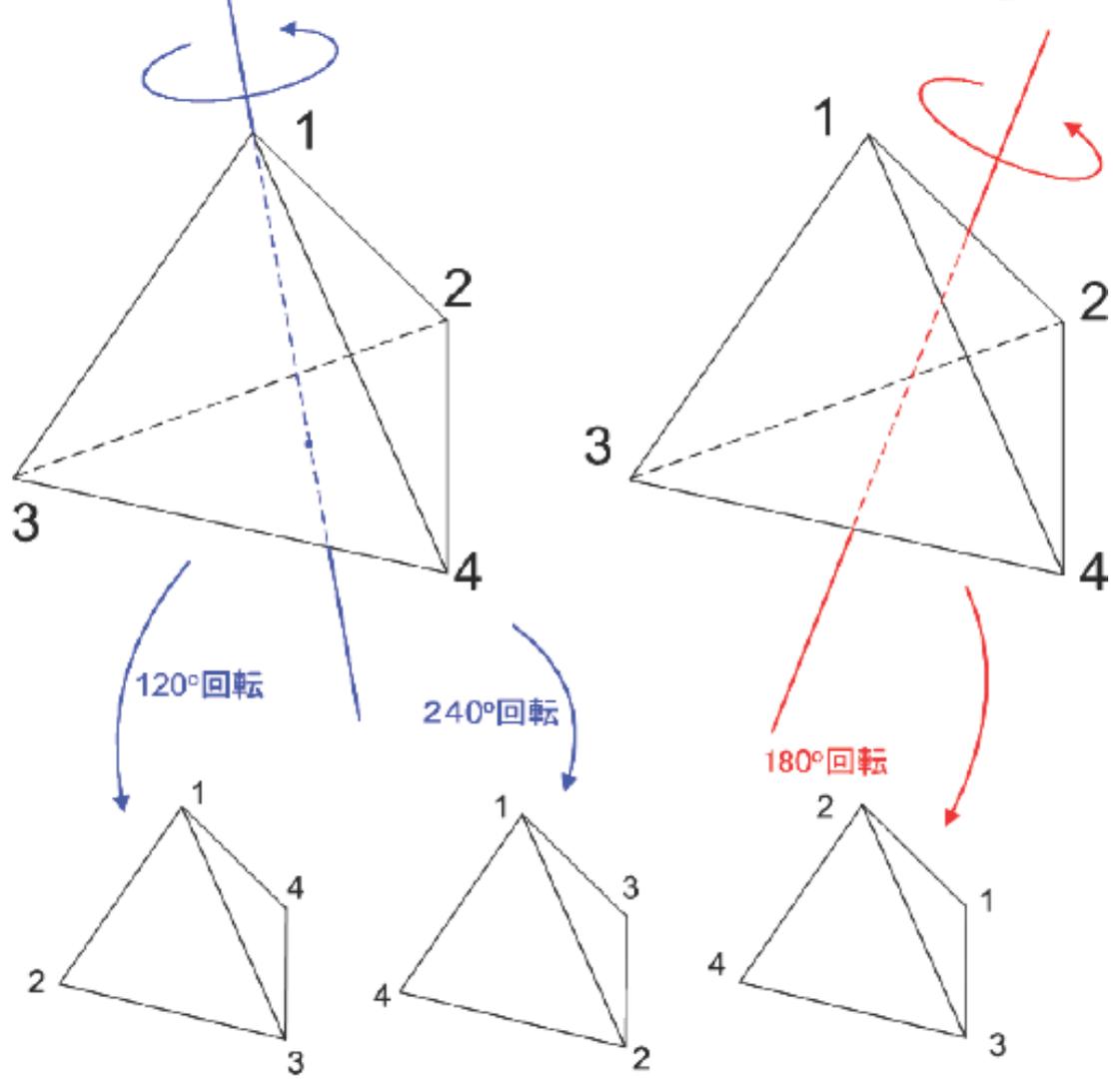
$$\tan^2 \theta_{12} = \frac{1}{2} \qquad \sin^2 2\theta_{23} = 1$$

$$\theta_{12} \doteq 35^\circ$$

$$\theta_{23} = 45^\circ$$

$$\theta_{13} = 0$$

# A4 flavor symmetry can easily realize (approximate or exact) Tri-Bi-maximal Mixing



**A4 symmetry**  
**(Tetrahedral Symmetry)**

# Tetrahedral Symmetry $A_4$

For 3 families, we should look for a group with a 3 representation, the simplest of which is  $A_4$ , the group of the **even** permutation of 4 objects.

class	$n$	$h$	$\chi_1$	$\chi_{1'}$	$\chi_{1''}$	$\chi_3$
$C_1$	1	1	1	1	1	3
$C_2$	4	3	1	$\omega$	$\omega^2$	0
$C_3$	4	3	1	$\omega^2$	$\omega$	0
$C_4$	3	2	1	1	1	-1

**1    1'    1''    3**

*by E. Ma*

$$\omega = \exp(2\pi i/3) = -1/2 + i\sqrt{3}/2$$

Multiplication rule:

$$\begin{aligned} \underline{3} \times \underline{3} &= \underline{1}(11 + 22 + 33) + \underline{1}'(11 + \omega^2 22 + \omega 33) \\ &+ \underline{1}''(11 + \omega 22 + \omega^2 33) + \underline{3}(23, 31, 12) + \underline{3}(32, 13, 21). \end{aligned}$$

Note that  $\underline{3} \times \underline{3} \times \underline{3} = \underline{1}$  is possible in  $A_4$ ,

i.e.  $a_1 b_2 c_3 + \text{permutations}$ ,

and  $\underline{2} \times \underline{2} \times \underline{2} = \underline{1}$  is possible in  $S_3$ ,

i.e.  $a_1 b_1 c_1 + a_2 b_2 c_2$ .

*by E. Ma*

## Approximate Tribimaximal Mixing

Fields	$L$	$F$	$\phi_1$	$\phi_2$	$\phi_3$	$\eta_1$	$\eta_2$	$\eta_3$	$\xi$
$A_4$	<b>3</b>	<b>3</b>	<b>1</b>	<b>1'</b>	<b>1''</b>	<b>1</b>	<b>1'</b>	<b>1''</b>	<b>3</b>
$SU(2)_L$	<b>2</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>2</b>	<b>3</b>	<b>3</b>	<b>3</b>	<b>3</b>
$Y$	-1	2	-1	-1	-1	2	2	2	2

$$L \text{ } l^c \Phi_i \quad 3 \times 3 \times (1, 1', 1'') \quad \leftarrow \text{Diagonal matrix}$$

$$L L \eta_i \quad 3 \times 3 \times (1, 1', 1'') \quad L L \xi \quad 3 \times 3 \times 3$$

$$m_e = h_1 v_1 + h_2 v_2 + h_3 v_3$$

$$m_\mu = h_1 v_1 + \omega h_2 v_2 + \omega^2 h_3 v_3$$

$$m_\tau = h_1 v_1 + \omega^2 h_2 v_2 + \omega h_3 v_3$$

$$\langle \Phi_i \rangle = v_1, v_2, v_3$$

$$\omega = \exp(2\pi i/3)$$

$$M_\nu = \begin{pmatrix} a + b + c & f & e \\ f & a + \omega b + \omega^2 c & d \\ e & d & a + \omega^2 b + \omega c \end{pmatrix}$$

$$a = \lambda_1 \langle \eta_1^0 \rangle \quad b = \lambda_2 \langle \eta_2^0 \rangle \quad c = \lambda_3 \langle \eta_3^0 \rangle$$

$$d = \kappa \langle \xi_1^0 \rangle \quad e = \kappa \langle \xi_2^0 \rangle \quad f = \kappa \langle \xi_3^0 \rangle$$

**Vacuum Alignment of  $\xi$  gives  $d=e=f$**

$$\mathcal{M}_\nu = \begin{pmatrix} a + b + c & d & d \\ d & a + \omega b + \omega^2 c & d \\ d & d & a + \omega^2 b + \omega c \end{pmatrix}$$

Assume  $b = c$  and rotate to the basis

$[\nu_e, (\nu_\mu + \nu_\tau)/\sqrt{2}, (-\nu_\mu + \nu_\tau)/\sqrt{2}]$ , then

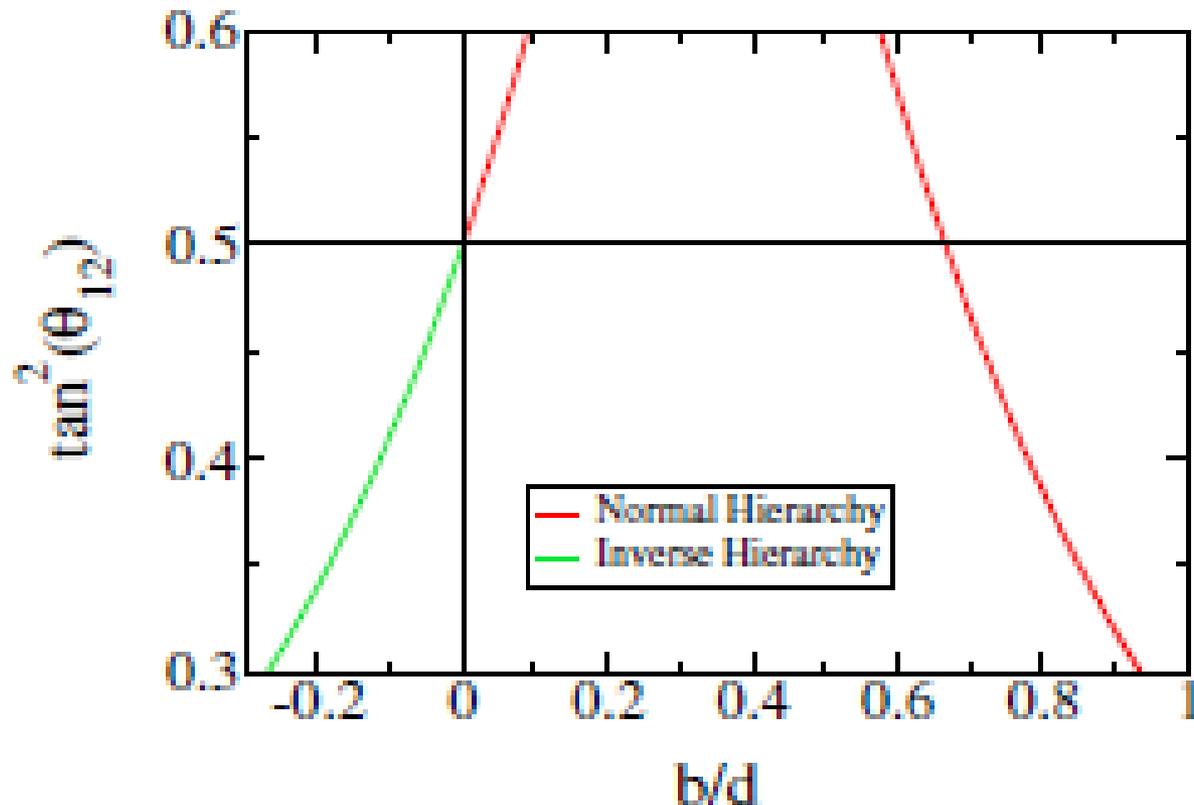
$$\mathcal{M}_\nu = \begin{pmatrix} a + 2b & \sqrt{2}d & 0 \\ \sqrt{2}d & a - b + d & 0 \\ 0 & 0 & a - b - d \end{pmatrix},$$

i.e. maximal  $\nu_\mu - \nu_\tau$  mixing and  $U_{e3} = 0$ .

$$t_{2s} = \tan(2\theta_{12}) = \frac{2\sqrt{2}d}{3b - d}$$

**depend on mass parameters**

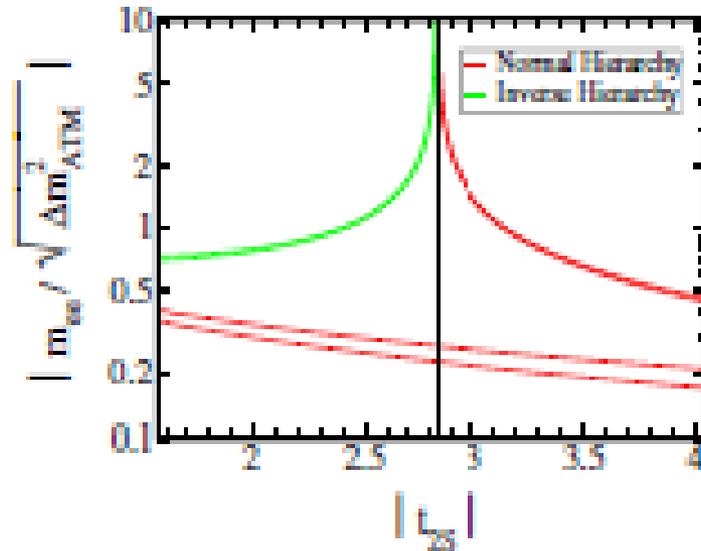
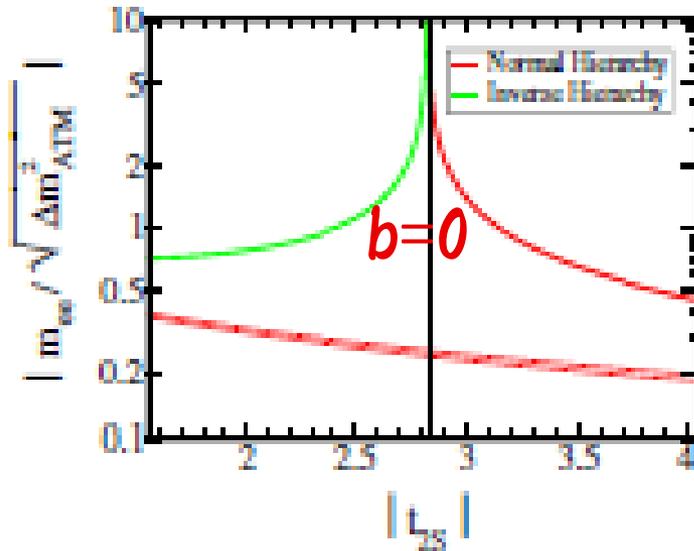
**Tri-Bi-Maximal mixings if  $b=0$  or  $b=2/3 d$**



$$\langle m_\nu \rangle = M_\nu(1, 1) = a + b + c = a + 2b$$

$$\frac{\Delta m_{\text{sol}}^2}{\Delta m_{\text{atm}}^2} = 0.022$$

$$0.065$$



**Lower Bound**

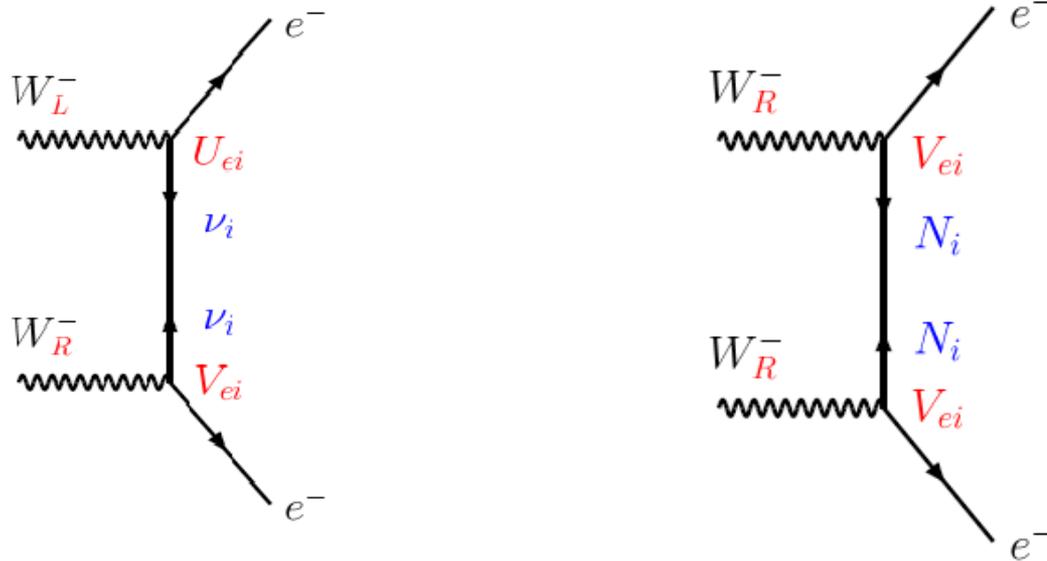
$$0.17 < |\langle m_\nu \rangle|/\sqrt{\Delta m_{\text{atm}}^2} \quad \text{for NH}$$

$$0.70 < |\langle m_\nu \rangle|/\sqrt{\Delta m_{\text{atm}}^2} \quad \text{for IH}$$

# 4 New Physics of Neutrinoless Double Beta Decay

## New Physics 1

### Right-handed W Bosons at 1 TeV Scale



$^{76}\text{Ge}$  half-life of  $T^{1/2} > 1.2 \times 10^{25}$  ys

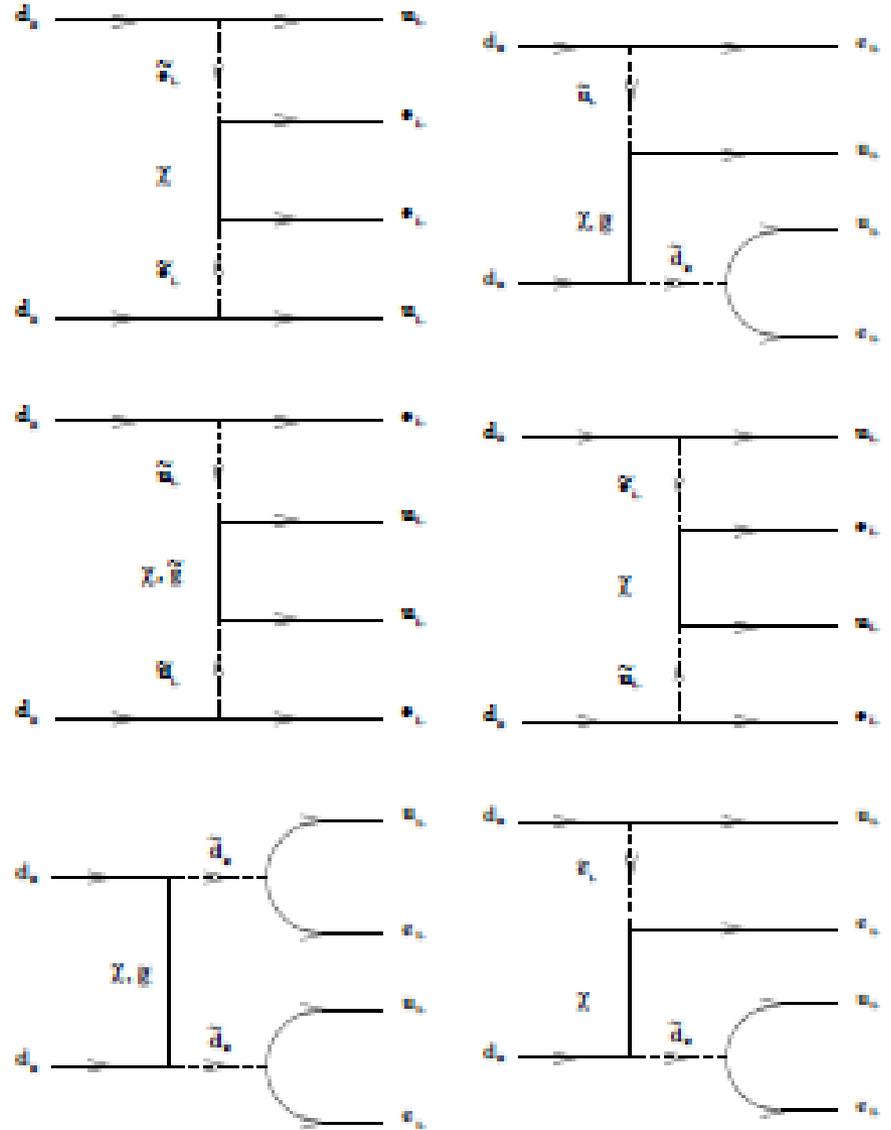
# New Physics 2

**Assume  
R-parity  
Violation  
In SUSY**

**Appear  
Lepton number  
violating terms**

$$\mathcal{L} = -\lambda'_{111} \left[ (\bar{e}_L \bar{\nu}_L)_j (d_R)_k \cdot \begin{pmatrix} \tilde{u}_L^* \\ -\tilde{d}_L^* \end{pmatrix}_j + \dots + h.c. \right]$$

$$\lambda'_{111} \leq 3.2 \times 10^{-4} \left( \frac{m_{\tilde{q}}}{100\text{GeV}} \right)^2 \left( \frac{m_g}{100\text{GeV}} \right)^{1/2}$$



# New Physics 3

## Sterile Neutrinos

A Yu.Smirnov, and R Z.Funchal , PRD74(2006)013001

$$\begin{pmatrix} m_a & m_{aS} \\ m_{aS}^T & m_S \end{pmatrix} \Rightarrow (m_\nu)_{ij} \simeq (m_a)_{ij} + (m_I)_{ij}$$

$m_a$  :  $3 \times 3$  active neutrino mass matrix

$$m_I \equiv -\frac{m_{aS}m_{aS}^T}{m_S} \quad \sin \theta_{jS} \approx \frac{m_{jS}}{m_S}$$

$$(m_I)_{ij} = -\sin \theta_{iS} \sin \theta_{jS} m_S \Rightarrow -\sin^2 \theta_S m_S$$

**if flavor blind mixing**

# New Physics 3

## Sterile Neutrinos

$$A^{(S)} \propto \frac{(m_I)_{ee}}{\bar{q}^2 - m_\nu^2} + \frac{m_S \sin^2 \theta_{eS}}{\bar{q}^2 - m_S^2}, \quad \bar{q} \approx 100 \text{MeV}$$

If  $m_S^2 \ll \bar{q}^2$ ,  $A^{(S)}$  is small due to  $(m_I)_{ee} = -\sin^2 \theta_{eS} m_S$  .

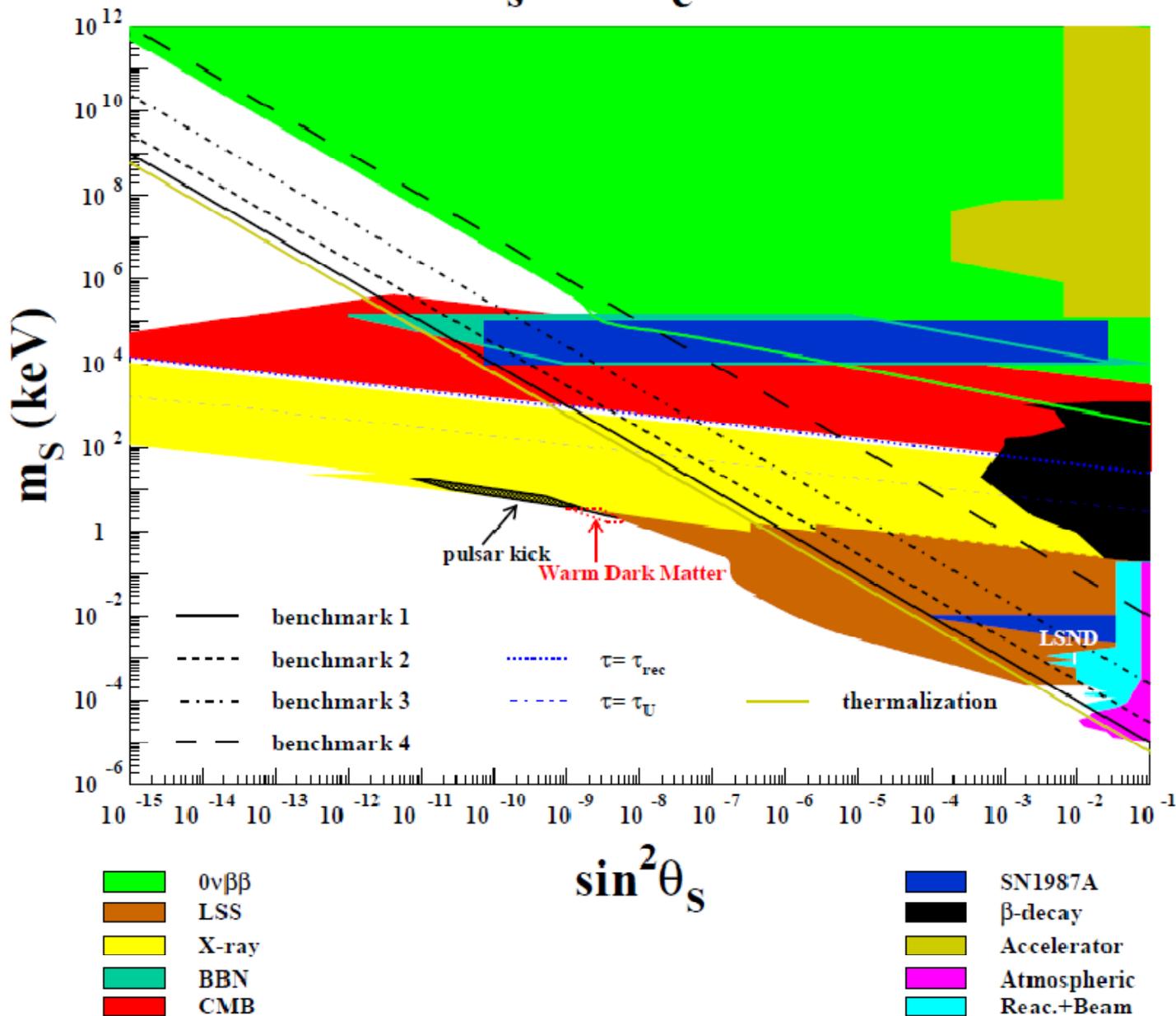
If  $m_S^2 \gg \bar{q}^2$ , **the second term is neglected.**

Since there is no cancellation, then  $\langle m_\nu^S \rangle = m_S \sin^2 \theta_{eS}$

Future bound  $\langle m_\nu \rangle < 30 \text{ meV}$

will improve the bound on  $\sin^2 \theta_{eS}$  by a factor 10.

$$\nu_s \leftrightarrow \nu_e$$



# 5 Future

## Are Neutrinos Majorana Particle ?

If yes, **L number is violated !**

**Leptogenesis can be realized.**

**“Origin of Baryon Asymmetry”**

**By measurement of  $\langle m_\nu \rangle$  :**

**Neutrino mass hierarchy is tested.**

**Some neutrino mass matrix is tested.**

**New physics bounds are given.**

If not, **Neutrino is Dirac Particle !**

**Why are neutrino masses tiny ? Extra Dimensions ?**

**Neutrinoless Double Beta Decay Experiments  
can give big answer “Majorana or not“ !**